

Granularity of co-Evolutions Patterns in Dynamic Attributed Graphs

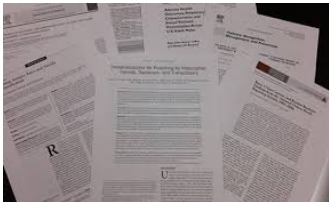


Elise Desmier, Marc Plantevit, Céline Robardet, Jean-François
Boulicaut

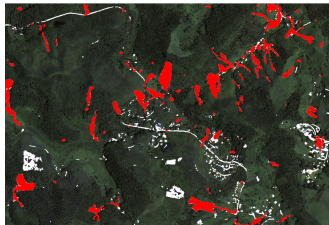
The Thirteenth International Symposium on Intelligent Data Analysis
(IDA 2014), Leuven, Belgium.



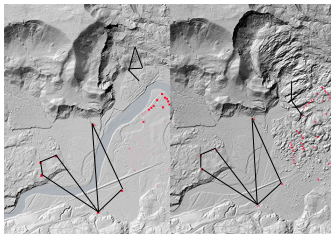
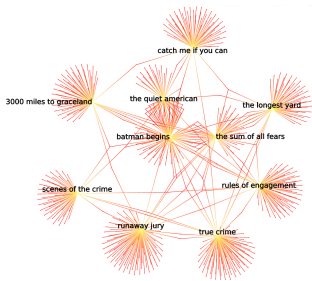
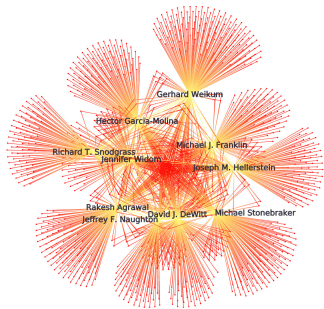
Data: a new “natural resource”



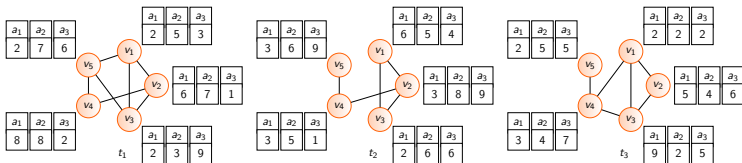
Potential increase of our knowledge



Viewed as dynamic attributed graphs



Objectives



Extract patterns from dynamic attributed graphs.



Entities



Interactions (social, spatial, etc.)



Dynamic



Entity information



Pattern that describes a local temporal phenomena

We propose to mine *maximal dynamic attributed sub-graphs* that satisfy some constraints on the *graph topology* and on the *attribute values*.

Overview of our proposal

Experimental results

DBLP US flights Brazil landslides



↓
Co-evolution patterns

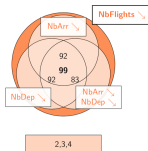


Interestingness Measures



(Desmier et al., ECML/PKDD 2013)

- Some obvious patterns are discarded ...
- ... but some patterns need to be generalized



Overview of our proposal

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Co-evolution patterns

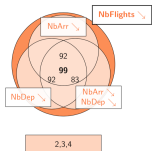


Interestingness Measures



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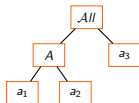
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Hierarchical co-evolution patterns

Take benefits from a hierarchy over the vertex attributes to :

- return a more concise collection of patterns;
- discover new hidden patterns;





Talk Outline

- 1 Co-evolution patterns
- 2 Hierarchical co-evolution patterns
- 3 Empirical study
- 4 Conclusion and perspectives

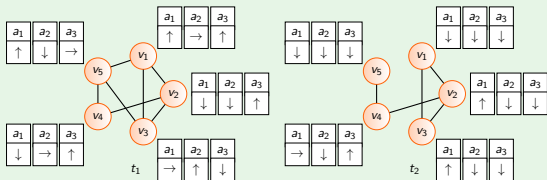


Dynamic Attributed Graphs

A dynamic attributed graph $\mathcal{G} = (\mathcal{V}, \mathcal{T}, \mathcal{A})$ is a sequence over \mathcal{T} of attributed graphs $G_t = (\mathcal{V}, E_t, A_t)$, where:

- \mathcal{V} is a set of vertices that is fixed throughout the time,
- $E_t \in \mathcal{V} \times \mathcal{V}$ is a set of edges at time t ,
- A_t is a vector of numerical values for the attributes of \mathcal{A} that depends on t .

Example

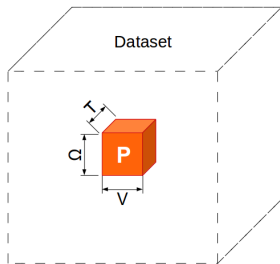




Co-evolution Pattern

Given $\mathcal{G} = (\mathcal{V}, \mathcal{T}, \mathcal{A})$, a co-evolution pattern is a triplet $P = (V, T, \Omega)$ s.t.:

- $V \subseteq \mathcal{V}$ is a subset of the vertices of the graph.
- $T \subseteq \mathcal{T}$ is a subset of not necessarily consecutive timestamps.
- Ω is a set of signed attributes, i.e., $\Omega \subseteq A \times S$ with $A \subseteq \mathcal{A}$ and $S = \{+, -\}$ meaning respectively a $\{increasing, decreasing\}$ trend.





Predicates

A co-evolution pattern must satisfy two types of constraints:

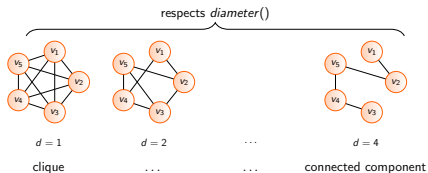
Constraint on the evolution:

- Makes sure attribute values co-evolve
- We propose δ -**strictEvol**.
- $\forall v \in V, \forall t \in T$ and $\forall a^s \in \Omega$ then δ -trend(v, t, a) = s



Constraint on the graph structure:

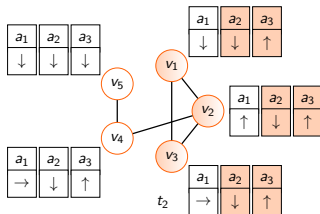
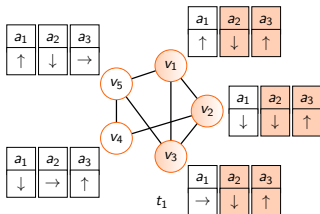
- Makes sure vertices are related through the graph structure.
- We propose **diameter**.
- Δ -diameter(V, T, Ω) = true $\Leftrightarrow \forall t \in T$ $\text{diam}_{G_t}(V) \leq \Delta$



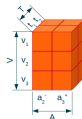


Example

$$P = \{(v_1, v_2, v_3)(t_1, t_2)(a_2^-, a_3^+)\}$$



- 1-Diameter(P) is true,
- 0-strictEvol(P) is true.

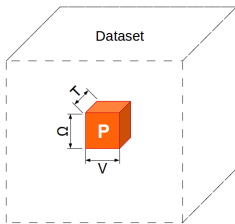




Density Measures

Intuition

Discard patterns that depict a behaviour supported by many other elements of the graph. We propose : **vertex specificity**, **temporal dynamic** and **trend relevancy**.





Talk Outline

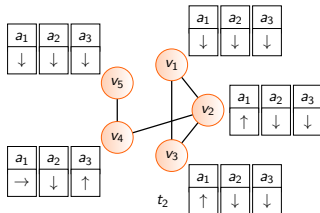
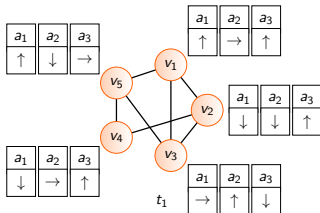
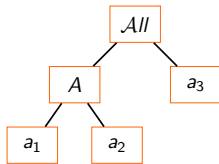
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Hierarchy

A hierarchy \mathcal{H} on \mathcal{A} is a tree where:

- the edges are a relation is_a ,
- the node All is the root of the tree,
- the leaves are attributes of \mathcal{A} ,
- $dom(\mathcal{H})$ is all the nodes except the root.

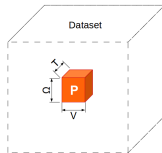




Hierarchical co-evolution Patterns

Given $\mathcal{G} = (\mathcal{V}, \mathcal{T}, \mathcal{A})$ and \mathcal{H} , a hierarchical co-evolution pattern is a triplet $P = (V, T, \Omega)$ s.t.:

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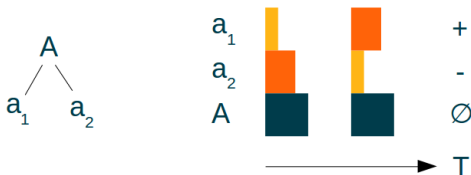
It must respect the following constraints:

- 1 Constraint on the evolution.
- 2 Constraint on the graph structure.



Evolution Constraint

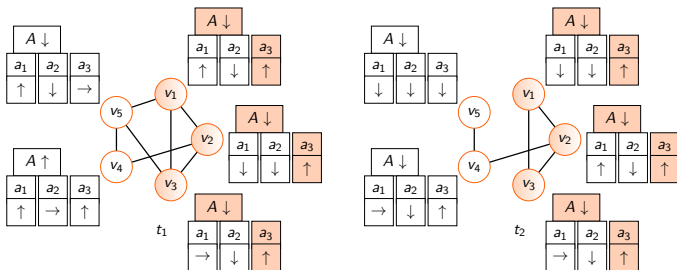
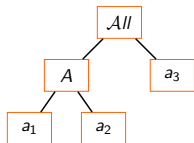
For an attribute A , its evolution is computed from the evolution of the leaves it covers.





Example

$$P = \{(v_1, v_2, v_3)(t_1, t_2)(A^-, a_3^+)\}$$



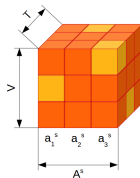
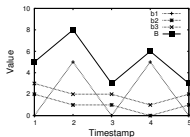
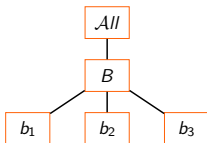
- 1-Diameter(P) is true,
- 0-strictEvolHierarchical(P) is true.



Purity of the pattern

Is the pattern described with the good level of granularity?

Purity computes the proportion of valid triplet (v, t, a^s) with regard to the number of possible triplets.

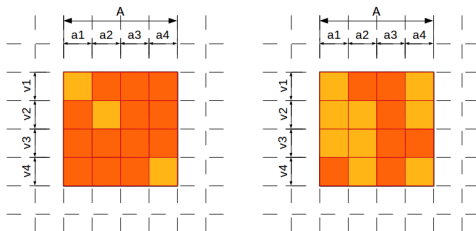


$$purity(P) = \frac{\sum_{v \in V} \sum_{t \in T} \sum_{a^s \in leaf(\Omega)} \delta_{a^s(v,t)}}{|V| \times |T| \times |leaf(\Omega)|}$$



Gain of purity

Does the pattern need to be specialized or kept generalized?



Keep attribute A

Specialize A to a_3

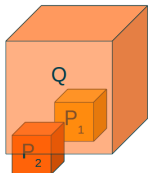
Gain measure compares the purity of the “children” pattern P with regard to the purity of its “parent” patterns.

$$gain(P) \Leftrightarrow \frac{purity(P)}{\max_{P_i \in parent(P)} (purity(P_i))} \geq \gamma$$



What about other measures/constraints?

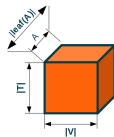
Maximality:



Size measures:



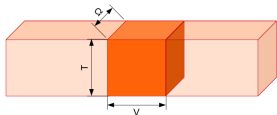
$$|leaf(A)| \geq min_A,$$



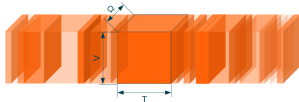
$$volume = |V| \times |T| \times |A|$$



Vertex specificity:



Temporal dynamicity:



No trend relevancy with hierarchies.

- What level of hierarchy do we consider?

- What about attributes discarded because of a too small purity gain?



Algorithm: Enumeration

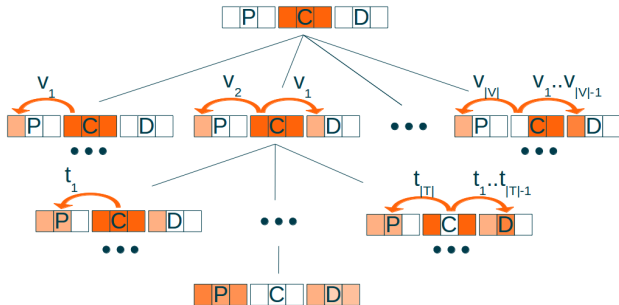
- $In(P)$: the pattern in construction
- $Cand(C)$: the elements not yet enumerated
- $Out(D)$: the elements enumerated as non member of the pattern

 $V T \Omega$

Full set

Partly full set

Empty set





Algorithm: Constraint Properties

How to use the properties of the constraints to reduce the search space?

Anti-monotonicity:

- strictEvol
- volume (bound with H)
- size measures

Piecewise anti-monotonicity:

- purity (bound)
- vertex specificity (bound with H)
- temporal dynamic (bound with H)
- trend relevancy (bound)

$f(\text{PUC}) > \sigma$ is anti-monotonic

$f(P) > \sigma$ is monotonic

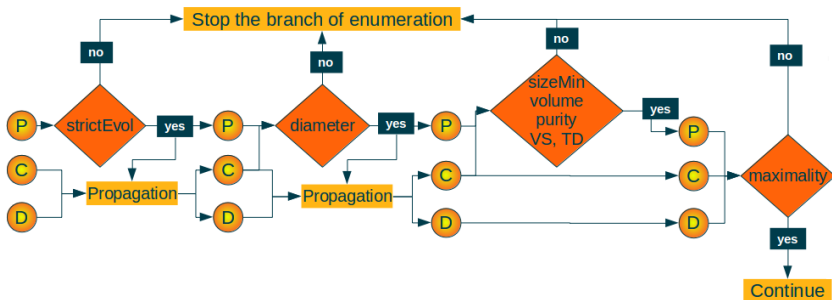
$f = \frac{a(\text{PUC})}{b(P)} > \sigma$ is piecewise anti-monotonic



Algorithm: Pruning and Propagation

Use the constraints at each step of the enumeration to

- prune: stop the branch of enumeration,
- propagate: discard elements from C and D.





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Quantitative Experiments

Co-evolution Patterns

Using relevancy constraints

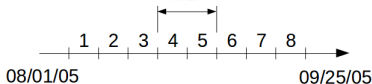
Hierarchical Co-evolution Patterns



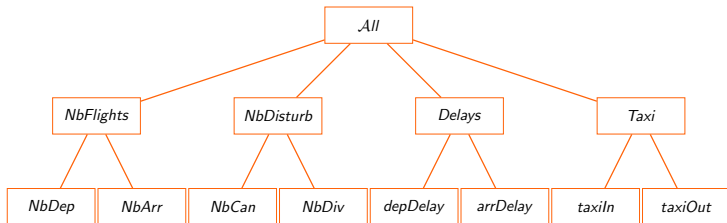
- ↘ Execution times
- ↘ Number of patterns
- ↗ Execution times
- ↘ Number of patterns



US flights datasets



- Vertices: 280 airports.
- Times: 8 weeks around the Katrina hurricane.
- Attributes: number of departure/arrival/cancelled/deviated flights, departure/arrival delays and ground times.

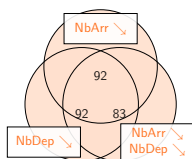


RITA "On-Time Performance" database.
 (<http://www.transtats.bts.gov>)

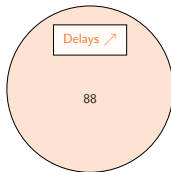


Hierarchy impact

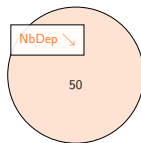
- 2 experiments with $\gamma = 1$ and $\gamma = 1.2$,
- Thresholds: $min_V=40$, $min_T=min_A=\vartheta=1$, $\psi=0.9$, $\kappa=0.2$, $\tau=0.4$.



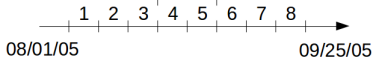
2,3,4



1,6,7



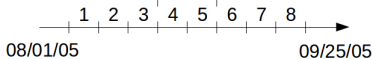
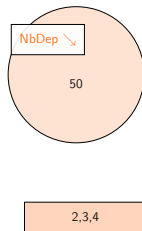
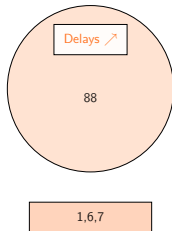
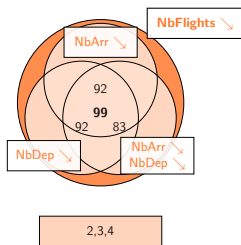
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Hierarchy impact

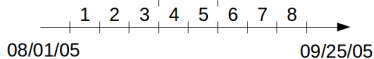
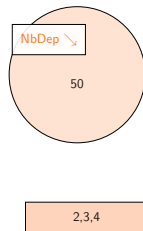
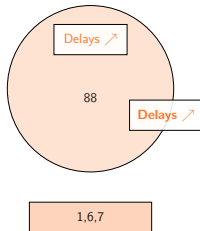
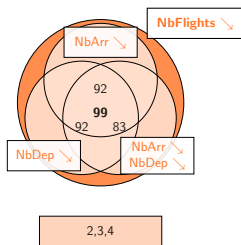
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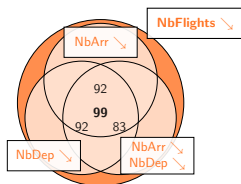
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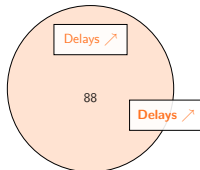


Hierarchy impact

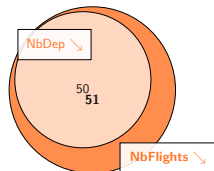
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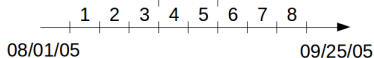
2,3,4



1,6,7



2,3,4





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Conclusion

We propose to extract hierarchical co-evolution patterns from a dynamic attributed graph and a hierarchy.

- These patterns are sets of vertices that are connected and that follow the same trends over a set of attributes over time, with attributes that are either those of the dataset or of the hierarchy.
- Definition of some constraints to reduce the execution time and increase the relevancy of the patterns, in particular according to hierarchy.
- Design of an algorithm to compute the complete set of patterns
- Experiments on a real-world dataset prove that this method extracts, in a feasible time, interesting patterns based on the user parametrized constraints.



Future Directions

Experimental results

DBLP US flights Brazil landslides



- Some obvious patterns are discarded ...
- ... but some patterns need to be generalized ✓
- Difficulties to set parameters.



Co-evolution patterns



Interestingness Measures



(Desmier et al., ECML/PKDD 2013)



Future Directions



Co-evolution patterns



Interestingness Measures



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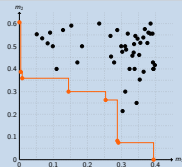
Experimental results

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⇒ Skyline Analysis



Thank you !



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