ABSTRACT

Materialized views can bring important performance benefits when querying XML documents. In the presence of XML document changes, materialized views need to be updated to faithfully reflect the changed document. In this work, we present an algebraic approach for propagating source updates to XML materialized views expressed in a powerful XML tree pattern formalism. Our approach differs from the state of the art in two important ways. First, it relies on set-oriented, algebraic operations, to be contrasted with node-based previous approaches. Second, it exploits state-of-the-art features of XML stores and XML query evaluation engines, notably XML structural identifiers and associated structural join algorithms. We present algorithms for determining how updates should be propagated to views, and highlight the benefits of our approach over existing algorithms through a series of experiments.

Categories and Subject Descriptors

H.2.4 [Database Management]: Systems

Keywords

XML view maintenance, XML updates, XML query processing

1. INTRODUCTION

XML data management has reached by now a certain level of maturity, with many commercial and open-source systems supporting the W3C’s XPath and XQuery [35] standards for querying XML documents. The complexity of XPath and XQuery and of the XML data itself raised many performance challenges. One direction of work towards improving the performance of XML query evaluation consists of relying on materialized views (or caches) storing precomputed query results, based on which queries can be answered more speedily than by using the original documents only [9, 18, 25, 29, 38]. Such techniques have been shown to improve query evaluation performance by up to several orders of magnitude.

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More recently, the W3C has also proposed an update extension to the XQuery language, namely XQuery Update [36]. XQuery Update is gradually being implemented in XML data management platforms. When materialized views are used as a performance-enhancing tool, updates to the XML database raise two new problems. First, one has to determine whether the result of a view should change due to the update (or, as often said, whether the update affects the view). This problem has been studied recently in [17, 12], and in the particular case when XML schemas are available to describe the documents in [9]. Second, when a view is indeed affected, a related issue is how to efficiently update the view to reflect the update. This second problem is the main focus of this paper.

Figure 1 illustrates the view maintenance problem in this context. Evaluating the view $v$ over the XML document $d$ leads to materializing $v(d)$. An XML update transforms $d$ into $d'$, and correspondingly the affected view $v$ should be transformed into $v(d')$. One possibility is to evaluate $v$ from scratch on the modified document $d'$. Instead, our focus is on incrementally modifying $v$ by adding, removing, or modifying data as needed, to transform it into $v(d')$, without recomputing it.

The incremental maintenance of XML materialized views has been considered in previous works [13, 10, 17, 18, 29, 28, 31]. Maintaining XML views over relational databases is studied in [16]. The maintenance of boolean XPath queries is studied in [13]. Views expressed in a richer XPath dialect are considered in [30, 31], which focus on node-level updates, that is, they consider updates which add or remove exactly one node to/from the document. Node-level updates are propagated to XQuery views in [17]. While node-level updates are conceptually simple, updates in real scenarios often involve more than one node. One reason is that by XQuery Update semantics, when node $n$ is inserted in document $d$, all descendants of $n$ become $d$ nodes, thus adding $n$ naturally leads to adding all its subtree. The same holds for deletions, i.e., removing $n'$ from $d$ automatically removes all the descendants of $n'$ from $d$. Another reason is that updates can be performed within for-loops where XQuery expressions, again applying many node-level updates through a single statement. Repeatedly applying node-level update propagation procedures may become inefficient. Thus, we focus on statement-level updates, and study how to propagate in one step all the changes entailed by a given XQuery update statement to the affected view. This problem was studied in [19] which proposes an XQuery algebra-based approach for maintaining XQuery views. However, that approach is defined in the Galax algebra and is thus quite tied to the internals of that system. More information on related works is provided in Section 6.

In our work, we address the incremental maintenance of XML views in the presence of statement-level XML updates. Our view...
language corresponds to a core useful conjunctive XQuery subset. This language supports the child and descendant axis, value and branch predicates, and moreover allows returning data from more than one node, unlike the XPath dialects studied in [13][30][31]. Our approach is designed to take advantage of advanced artifacts of current XML query processors, such as structural joins and smart identifiers [37]. Employing such efficient tools allows our algorithms to outperform node-level update propagation techniques in the frequent case where more than one node is added/removed at the same time. Moreover, our approach integrates smoothly in the process of updating the source document itself, by re-using some partial results of the update process. These features make it a good candidate to be integrated within a persistent XML database.

This paper is organized as follows. Section 2 presents our model for documents, views, and updates. Section 3 provides algorithms for propagating insertions, whereas Section 4 studies deletions. We conclude.

2. PRELIMINARIES

In this Section, we present our model for documents, node identifiers, views, and updates.

2.1 XML documents and node identifiers

We view XML documents as ordered label trees, consisting of element, attribute and text nodes. Element nodes and attribute nodes have a label, text nodes have an associated string representing the value. Each node has a unique identifier (or ID, in short), which is given by a compact unique string in the corresponding encoding scheme. Among the many node ID schemes from the literature, we use the recently proposed compact dynamic Dewey IDs [37] since they have many properties useful in our context:

- they are structural, i.e., by comparing two nodes, it is possible to know whether one is a parent (or ancestor) of the other;
- from the ID of a node, one may extract the IDs and labels of its ancestors at all levels;
- they do not require node relabeling in the presence of updates to the document;
- they can be encoded in a very compact fashion.

2.2 Views

Let \( \mathcal{L} \) be a finite set of XML node names, and \( \mathcal{XP} \) be the XPath [7] language. We consider views expressed in the XQuery dialect described in Figure 2. In the for clause, \( absVAR \) corresponds to an absolute variable declaration, which binds a variable named \( x \), to a path expression \( p \in \mathcal{XP} \) to be evaluated starting from the root of some document available at the URI \( \text{uri} \). The non-terminal \( relVAR \) allows binding a variable named \( x \) to a path expression to be evaluated starting from the bindings of a previously introduced variable \( x \). The optional where clause is a conjunction over a number of predicates, each of which compares the string value of a variable \( x \), with a constant \( c \).

The return clause builds, for each tuple of bindings of the for variables, a new element labeled \( l \), having some children labeled \( i \) \((l, i, \in \mathcal{L})\). Within each such child, we allow one out of three possible information items related to the current binding of a variable \( x \), declared in the for clause: (1) \( x \) denotes the full subtree rooted at the binding of \( x \); (2) \( \text{string}(x) \) is the string value of the binding; (3) \( \text{id}(x) \) denotes the ID of the node to which \( x \) is bound.

There are important differences between the subtree rooted at an element (or, equivalently, its content), its string value and its ID. The content of \( x \) includes all (element, attribute, or text) descendants of \( x \), whereas the string value is only a concatenation of \( x \)'s text descendants [38]. Therefore, \( \text{string}(x) \) is very likely smaller than \( x \)'s content, but it holds less information. Second, an XML ID does not encapsulate the content of the corresponding node. However, XML IDs enable joins which may stitch together tree patterns into larger ones. Our view dialect distinguishes IDs, value and contents, and allows any subset of the three to be returned for any of the variables, resulting in significant flexibility.

Tree pattern representation for views For ease of explanation, we represent views using the following tree pattern dialect, denoted \( \mathcal{P} \).

1. Pattern nodes can carry the label of an XML element or attribute, or some word, respectively. A word is defined as a sequence of characters appearing either in a PCDATA node or in an attribute value, delimited by the usual separators (whitespace, tab, end of line). Each internal pattern node carries a label from a tag alphabet \( A_t = \{a, b, c, \ldots\} \). Each leaf node carries a label from a word alphabet \( A_w = \{a, b, c, \ldots\} \).

2. Pattern edges correspond to parent-child or ancestor-descendant relationships between nodes.

3. Each pattern node may be annotated with stored attributes, describing additional information items that the pattern stores out of each XML document node, that matches the pattern node. The \( cont \) annotation indicates that the full (serialized) image matching the XML tree node is stored. The ID annotation indicates the Compact Dynamic Dewey ID [37] of the corresponding nodes. Storing IDs in views enables combining several views in order to answer a query [27][33]. Finally, the \( val \) annotation stands for the node’s text value, obtained by concatenating all its text descendants in document order.

4. Each node may be annotated with a predicate of the form \( \text{val} = c \) where \( c \in A_w \) restricting the XML nodes which match the pattern node, to those satisfying the predicate.
pred ≺≺ b
cuss a logical algebra here, and make no assumptions on how ≺ elimination (denoted ≺≺ parent of the node whose ID is the right-hand argument. Similarly, d ∈ R tuple in a view a derivation count semantics. In keeping with the standard literature on view maintenance, we also use joins, defined, as usual, as selections over (call it δ). After duplicate elimination (≺≺), we sort the tuples in the order of appearance of the corresponding nodes in d. We denote by ≺ parent comparison operator, which returns true if its left-hand argument is the ID of a parent of the node whose ID is the right-hand argument. Similarly, ≺ is the ancestor comparison operator. Observe that we only discuss a logical algebra here, and make no assumptions on how ≺ and ≺ are actually implemented in a physical store.

Let A be the algebra consisting of the following operators: (1) the n-ary cartesian product ×; (2) selection, denoted σ_{pred}, where pred is a conjunction of predicates of the form a ⊕ c or a ⊓ b, and a and b are attribute names, c is some constant, and ⊕ is a binary operator among {=, ⊆, ⊇}; (3) projection denoted π_{cols}; (4) duplicate elimination (denoted δ); (5) sort, denoted π_{sort}. For convenience, we also use joins, defined, as usual, as selections over ×.

The algebraic semantics of the tree pattern in Figure 3 is the algebraic expression in Figure 4. Reading from the bottom up, there is an R_{a} atom per query node labeled a, and they are connected through × operators. The selection σ enforces (i) all value constraints on the nodes, and (ii) all structural ≺ or ≺ relationships between query nodes. The projection retains the attributes projected by query nodes, e.g. paper.ID, affiliation.ID and affiliation.cont, but also the identifiers of all nodes annotated with some attribute. After duplicate elimination (δ), we sort the tuples in the order dictated by the IDs of the bindings of all nodes.

Derivation count A final important note is needed on the view semantics. In keeping with the standard literature on view maintenance for relational and XML data [22][31], we associate to each tuple in a view a derivation count, which intuitively corresponds to the number of reasons why the tuple belongs to the view. In the semantics based on embeddings, the number of derivations of a tuple t corresponds to the number of distinct embeddings of the view in a document, that lead to the same view tuple t. In our algebraic semantics, the derivation count of t is the number of tuples in the output of the δ operator which lead to obtaining t.

We end by noting that the semantics (content) of a view v (corresponding to a tree pattern) on a document d, together with the derivation numbers, can be computed in O(|v| × |d|), e.g. by an extension to the algorithm presented in [15].

2.3 Updates

We consider the following kinds of updates:

- delete q, where q is an XPath query from \( \mathcal{X} \mathcal{P} \);
- for \( \mathbf{x} \) in q insert xml into \( \mathbf{x} \), where \( \mathbf{q} \in \mathcal{X} \mathcal{P} \), and xml is a forest of XML trees. This generalizes to updates of the form for \( \mathbf{q}_1 \) insert \( \mathbf{q}_2 \) into \( \mathbf{x} \), where \( \mathbf{q}_1 \) is any XQuery, and \( \mathbf{q}_2 \) is an XPath query from \( \mathcal{X} \mathcal{P} \) as follows. First, we evaluate \( \mathbf{q}_1 \) on the original document, and then we proceed as if we were inserting \( \mathbf{q}_2 \) results as children. Of course \( \mathbf{q}_2 \) may depend on \( \mathbf{x} \), in which case different forests may be inserted under different nodes returned by \( \mathbf{q}_1 \).
- the simpler form insert xml into q with \( \mathbf{q} \in \mathcal{X} \mathcal{P} \) as above is also supported, together with its more general variant insert \( \mathbf{q}_1 \) into \( \mathbf{q}_2 \) where \( \mathbf{q}_1, \mathbf{q}_2 \in \mathcal{X} \mathcal{P} \).

3. PROPAGATING INSERTIONS

Let \( v \) be a view and \( u \) be an insert update directive on document d. In this Section, we discuss algorithms for transforming \( v \to u \) so as to reflect the effect of \( u \) on d. Section 3.1 outlines our general approach, then Section 3.2 describes a set of techniques which reduce the view maintenance effort, and Section 3.3 outlines how schema information can be used for further pruning. Section 3.4 introduces a set of useful ingredients for our algorithms, based on state-of-the-art XML query and update processing. Finally, Section 3.5 shows how to propagate updates which lead to adding new tuples to a view, whereas Section 3.6 considers the case when an XML insertion only leads to modifying view tuples.

3.1 Approach

Our approach relies on the algebraic view semantics, as follows. Assume that the nodes in the view v are labeled with the tags \( a_1, a_2, \ldots, a_k \in A_t \). Then, v can be written as:

\[
v = v_1(\sigma_{a_1}(R_{a_1}) \bowtie \sigma_{a_2}(R_{a_2}) \bowtie \ldots \bowtie \sigma_{a_{k}}(R_{a_{k}}))
\]

where for each \( a_i, \sigma_{a_i} \) is the possible selection on the value of the nodes matching the respective view node, and \( v_1 \) is an algebraic expression including the remaining projections, sorting steps, and duplicate eliminations in the full algebraic semantics of v. The joins \( \bowtie \) correspond to the specific structural relationship predicates connecting the a_i nodes in the view v.

We designate the nodes added by u to d as new nodes. For any node label \( l \), we term \( \Delta^{+}_l \) the ordered collection of tuples of the form (n.ID, n.val, n.cont) obtained from all the nodes n added to the document by the update. The IDs of the new nodes are computed as a side-effect of the document update, whereas their values and contents can be extracted directly from the subtrees rooted at the nodes (recall that according to the XQuery update semantics, when a node n is added to d, all the subtree of n is added to d). Based on the \( \Delta^{+}_l \) relations, the impact of u on d can be expressed as follows: for each node label \( l \) occurring in v, replace \( R^{d}_l \) by \( R^{d}_l = R^{d}_l \cup \Delta^{+}_l \).

After the update, the content of the view v should thus become:
\[ v' = v(d') = e_v(\sigma_{a_1}(R_{a_1} \cup \Delta^+_{u_1}) \bowtie \sigma_{a_2}(R_{a_2} \cup \Delta^+_{u_2}) \bowtie \ldots \bowtie \sigma_{a_{n-1}}(R_{a_{n-1}} \cup \Delta^+_{u_{n-1}}) \bowtie \sigma_{a_n}(R_{a_n} \cup \Delta^+_{u_n})) \]

To solve our incremental view maintenance problem, we will ignore \( e_v \), which is the part of \( v' \)’s algebraic semantics that applies projections, sorts, and eliminates duplicate tuples, because maintaining \( e_v \)'s output is straightforward once updates have been propagated to \( e_v \)'s input. Instead, we will focus on efficiently computing the join-over-union expression which builds the input to \( e_v \). To ease presentation, and without loss of generality, we may simply ignore \( e_v \) in the following examples. However, we underline that \( e_v \) is necessary to correctness of the semantics.

Distributing the joins over unions in the expression above leads to a single union of \( 2^k \) terms, each of which is a join expression. One of them involves no \( \Delta^+ \) relation, and corresponds to the original view \( v \). Propagating \( u \) thus requires computing the remaining \( 2^k - 1 \) union terms.

**Example 3.1.** Let \( d \) be a document and \( u_1 \) be an update that inserts in \( d \) the following XML snippet:

\[ \text{xml1} = (a/b)(b/c)/b/a \]

Let \( a_1, b_1, b_2 \) and \( c_1 \) be the XML elements inserted in \( d \) by \( u_1 \). The \( \Delta^+ \) relations corresponding to \( u_1 \) are:

<table>
<thead>
<tr>
<th>( \Delta^+ )</th>
<th>transformation</th>
</tr>
</thead>
<tbody>
<tr>
<td>( (a_1, id, a_1, val, a_1, cont) )</td>
<td>( (b_1, id, b_1, val, b_1, cont) )</td>
</tr>
<tr>
<td>( (b_2, id, b_2, val, b_2, cont) )</td>
<td></td>
</tr>
</tbody>
</table>

Consider the view \( v_1 = /a/b/a/c_1 \). After \( u_1 \) is applied, \( v_1 \) should become:

\[ u_1 \cup (R_a \bowtie_{a < c} b_1 R_b \bowtie_{b < a} c_1 R_c \bowtie_{c < a} \Delta^+) \cup (R_a \bowtie_{a < c} b_2 R_b \bowtie_{b < a} c_1 R_c \bowtie_{c < a} \Delta^+) \cup (R_a \bowtie_{a < c} b_1 R_b \bowtie_{b < a} c_2 R_c \bowtie_{c < a} \Delta^+) \cup (R_a \bowtie_{a < c} b_2 R_b \bowtie_{b < a} c_2 R_c \bowtie_{c < a} \Delta^+) \]

For brevity, in the sequel, we will omit the join predicates (which are always those of the view) from the union terms. Thus, the expected content of \( v_1 \) after the insertion in Example 3.1 can be written as:

\[ v_1 = R_a R_b \Delta^+ \cup R_a \Delta^+ R_b \cup R_b \Delta^+ R_c \cup R_a \Delta^+ R_c \cup \Delta^+ R_b \Delta^+ R_c \cup \Delta^+ R_a \Delta^+ R_c \cup \Delta^+ R_a \Delta^+ R_b \]

In the remainder of this Section, we study practical algorithms for computing the \( 2^k - 1 \) terms whose results need to be added to \( v \) in order to make it reflect the insertion.

### 3.2 Term pruning

Several observations lead us to infer when some of the union terms are guaranteed to have empty results. Such union terms are *pruned*, that is, their evaluation is not necessary in order to propagate the insertion to the view. Pruning significantly reduces the update propagation effort.

**Pruning by the update semantics.** The semantics of XQuery Update allows deciding that some terms will always have empty results. Intuitively, this is because XQuery updates allow adding new children to existing nodes, but not new parents, as the following example illustrates.

**Example 3.2.** Consider the insertion \( u_1 \) from Example 3.1. A newly added node cannot have as child a \( b \) node which belonged to \( d \) before \( u_1 \) was applied. Thus, \( \Delta^+_{u_1} R_a \) is empty, therefore the terms \( \Delta^+_{u_1} R_a R_b \) and \( \Delta^+_{u_1} R_b \Delta^+_{u_1} \) to be added to \( v_1 \) in order to maintain it are guaranteed to produce an empty result. Similarly, no \( b \) element in \( \Delta^+_{u_1} \) can have descendants in \( R_a \), therefore \( \Delta^+_{u_1} R_a \Delta^+ \cup \Delta^+_{u_1} R_b \Delta^+ \cup \Delta^+_{u_1} \Delta^+ \) is also empty, and so are \( R_a R_b \Delta^+ \) and \( \Delta^+_{u_1} R_a \Delta^+ \). Thus, to compute \( v_1 \), it suffices to add to \( v \) the results of evaluating the terms:

\[ (*) R_a R_b \Delta^+ \cup R_a \Delta^+ \cup \Delta^+ \cup \Delta^+ \Delta^+ \Delta^+ \]

This observation is generalized by the following proposition:

**Proposition 3.3.** Let \( v \) be a view of \( k \) nodes, and \( n_1, n_2 \) be nodes such that \( n_2 \) is a \( / \) or \( // \) child of \( n_1 \). Let \( R_{n_1} \), respectively, \( R_{n_2} \) be the atoms corresponding to \( n_1 \), respectively, \( n_2 \) in the algebraic semantics of \( v \), i.e., \( R_{n_1} \bowtie_{n_1} R_{n_2} \) is a sub-expression of \( v \).

Let \( v \) be an arbitrary insertion, and \( t \) be one of the \( 2^k - 1 \) terms to be added to \( v \) in order to propagate the effect of \( u \). If \( t \) contains as a sub-expression \( \Delta^+ \) \( R_{n_2} \), then \( t \) produces an empty result.

Observe that Proposition 3.3 does not depend on the insertion \( u \). Therefore, in the sequel, when propagating updates to a view, we only focus on the terms which have survived this pruning.

**Inserted data-driven pruning.** Inspecting the XML fragments to be inserted in the document may allow further pruning, as illustrated by the following example:

**Example 3.4.** Consider the view \( v_1 \) from Example 3.1 and the insertion \( u_2 \) which adds the following XML snippet:

\[ \text{xml2} = (a/b)(b/c)/b/a \]

The difference with respect to Example 3.1 is that \( \text{xml2} \) does not include a \( c \) element, i.e., \( \Delta^+ c = \emptyset \). This entails that all the terms of the expression (*) in Example 3.2 are empty and thus, \( v_1 \) is not affected by \( u_2 \).

Value predicates may also impact update propagation, as the following example shows:

**Example 3.5.** Consider the view \( v_2 = /a/var=5//b/a \) and the insertion \( u_3 \) adding the following XML snippet:

\[ \text{xml3} = (a/5/b)/b/a \]

In this case, \( \Delta^+ \neq \emptyset \) and \( \Delta^+ \neq \emptyset \), however \( \sigma_{\text{val}=5}(\Delta^+) = \emptyset \) because the new element does not satisfy the view predicate \( \text{val} = 5 \). Thus, \( R_a \Delta^+ \Delta^+ \) and \( \Delta^+ \Delta^+ \), which both involve \( \sigma_{\text{val}}(\Delta^+) \), are empty. Since Proposition 3.3 the term \( \Delta^+ R_a \) is also empty, \( v_2 \) is unaffected by \( u_3 \).

This generalizes to the following simple observation:

**Proposition 3.6.** Let \( u \) be an insertion adding the trees \( t_1, t_2, \ldots, t_k \) to \( d \), and \( v \) be a view. If a node \( n \) of \( v \) is not matched in any of the trees \( t_1, t_2, \ldots, t_k \), all union terms involving \( \Delta^+ n \) are empty.
**Inserted ID-driven pruning.** A third pruning criteria takes advantage of an interesting property of Compact Dynamic Dewey IDs [17]:

**Example 3.7.** Consider the view \( v_1 \) from Example 3.7 and the insertion \( u_4 \), adding the following XML snippet:

\[
\text{xml}_4 = (b)(c)\text{/}(b)
\]
as a child of a node \( a \), whose ID is \( a.id \). This ID encodes the labels of all the nodes on the path from \( a \) to the root [17]. Assume that we inspect \( a.id \) and find that no ancestor labeled \( b \) appears above the \( a \) node. Then, the new (inserted) \( c \) node has only one \( b \) ancestor, namely the inserted (new) \( b \) node. Thus, the term \( R_a R_b \Delta^+_c \) in (*) is empty.

In this example, moreover, since \( \Delta^+_a = \emptyset \), the term \( \Delta^+_a \Delta^+_b \Delta^+_c \) in (*) is also empty. Thus, the only term we need to compute to update \( v_1 \) after inserting \( \text{xml}_4 \) is: \( R_a \Delta^+_b \Delta^+_c \).

This generalizes as follows:

**Proposition 3.8.** Let \( u \) be an insertion adding children to the nodes \( p_1, p_2, \ldots, p_k \) in \( d \). Let \( v \) be a view, and \( n_1, n_2 \) be \( v \) nodes such that \( n_1 \) is an ancestor of \( n_2 \) in \( v \).

If for each \( i = 1, 2, \ldots, k \), \( p_i \) is not labeled \( n_1 \) and has no ancestor labeled \( n_2 \), then all union terms containing \( R_{n_1} \Delta_{n_2} \) are empty.

### 3.3 Exploiting schema information

A schema for XML documents might not always be available, nor is the programmer expected to write update statements that are valid with respect to a schema. When document type information is available, we can use it in our approach to either reject some schema-violating insertions, or optimize their propagation. The first issue (deciding view-update independence) is not our main focus and has been thoroughly considered elsewhere [7, 10]. We present in this section the kind of run-time independence decisions that our framework captures. Our techniques rely on the inserted data, thus they may require partially evaluating the update (as opposed to purely static techniques using only the update statement and the view). Being inspired by real update scenarios, we thought that it could have been useful to make these decisions at run-time and actually let the user choose to proceed or not with update propagation, in the presence of schema violations. In practice, static and run-time checks are complementary and can be combined to reduce view maintenance effort whenever possible. Dealing with such a combination is beyond the scope of our work.

**Deciding view-update independence** We consider that documents are characterized by DTDs expressed as extended context-free grammars (CFGs), where the right-hand side of each rule is a regular expression over an alphabet of terminal and non-terminal symbols. For instance, Figure 5 depicts two DTDs. In this figure, \( a \), \( b \), \( c \), \( d_1 \), \( d_2 \) and \( x \) are terminal symbols and \( \text{AS} \) and \( \text{BS} \) are non-terminal ones. DTD \( d_1 \) (a) has mandatory edges, while DTD \( d_2 \) (b) features concatenation, disjunction and recursion.

**Example 3.9.** Consider the view \( v_1 \) from Example 3.7 and an insertion \( u_5 \), adding the following XML snippet:

\[
\text{xml}_5 = (a)(b)\text{/}(b)/(a)
\]

Applying the update would make the document invalid with respect to the DTD in Figure 5 (a), since a \( c \) element is missing under \( b \). More generally, from the DTD \( d_1 \), one can derive that the following statement must hold for any newly inserted XML tree:

\[
\Delta^+_a \neq \emptyset \Rightarrow (\Delta^+_a \neq \emptyset \land \Delta^+_c \neq \emptyset)
\]

Since this does not hold on the update \( u_5 \), we reject it due to its attempted schema violation.

The same consideration applies to Figure 5 (b), in which a \( d_2 \) element must have as children the concatenation of an \( a \) and \( b \). Therefore, any insertion of an \( a \) element under the root \( d_2 \) must occur with \( b \) and \( c \) elements.

**Example 3.10.** The DTD in Figure 5 (b) implies that the following statement must hold on any XML forest inserted under a given node:

\[
\Delta^+_a \neq \emptyset \Rightarrow (\Delta^+_a \neq \emptyset \land \Delta^+_c \neq \emptyset)
\]

More generally, from the DTD rules, one can infer a set of constraints on the \( \Delta^+_a \) tables, and check them before applying the update. If any constraint is violated, the update is rejected.

### 3.4 Helper functions and operators

Let \( u \) be an update (insertion or deletion), and \( \text{pul}(u) \) be the pending update list [36] resulting from \( u \). Thus:

- if \( u \) is an insertion, \( \text{pul}(u) = \{(n_1, t_1), (n_2, t_2), \ldots, (n_k, t_k)\} \), a list of pairs consisting of an XML element \( n_i \) target of the update, and a subtree \( t_i \) to be copied as a child of \( n_i \).
- if \( u \) is a deletion, \( \text{pul}(u) = \{n_1, n_2, \ldots, n_k\} \) is the list of the nodes to be removed.

We assume available:

- **compute-pul(\( u \))** A procedure which from an update \( u \), computes its pending update list \( \text{pul}(u) \). Any XQuery Update-compliant store has (some version of) this procedure.

- **apply-insert(\( n, t \))** is a function which, given a node \( n \) and a tree \( t \) to be copied as a child of \( n \) copies \( t \) as a new child of \( n \) and returns the tree \( t' \) created by the copy operation. Importantly for us, the tree \( t' \) also includes the IDs assigned to the copied nodes in their new context (in \( d \)).

- **extr-pattern(\( p, t \))** is a function which, given a tree pattern \( p \) and an XML tree \( t \), evaluates \( p \) on \( t \) and returns the corresponding set of tuples. An \( O(|p| \times |t|) \) implementation of **extr-pattern** is obtained by extending the algorithm presented in [15].

**operators** We also assume available the following logical (and physical) operators:

**Structural Joins** comprise the classical Stack Tree Ancestor and Stack Tree Descendant algorithms [2].

<table>
<thead>
<tr>
<th>DTD</th>
<th>Expression</th>
<th>View Update Independence</th>
</tr>
</thead>
<tbody>
<tr>
<td>( d_1 )</td>
<td>( AS \rightarrow d_2 \rightarrow AS )</td>
<td>Valid</td>
</tr>
<tr>
<td>( d_2 )</td>
<td>( a \rightarrow \text{BS} \rightarrow \text{BS} )</td>
<td>Valid</td>
</tr>
<tr>
<td>( d_2 )</td>
<td>( b \rightarrow e )</td>
<td>Invalid</td>
</tr>
</tbody>
</table>

**Figure 5:** Sample DTDs, expressed as CFGs.

\[
\Delta^+_a = \emptyset \Rightarrow (\Delta^+_a \neq \emptyset \land \Delta^+_c \neq \emptyset)
\]
Algorithm 1: Propagate Insert by New Tuples (PINT)

Input : view v, insert update u
Output: updated view v’ to reflect u
1 Develop the $2^n - 1$ union terms to be added to v in case of insertions, and prune them based on XQuery update semantics (Proposition 3.3)
2 Compute the $\Delta^+$ tables corresponding to v
3 Further prune terms based on the $\Delta^+$ tables (Propositions 3.6 and 3.8)
4 Evaluate the remaining terms and add their results to v
5 If needed, update auxiliary structures

- **Path Filter** allows checking whether a node having a specific ID is on a path satisfying a specific condition.
- **Path Navigate** allows to obtain, from the ID of some nodes, the IDs of their parents.

The PathFilter and PathNavigate are implemented by exploiting the information encapsulated by the expressive node IDs we use [27].

### 3.5 Propagating insertions by adding tuples to the view

Our first update propagation algorithm considers the cases when an insertion to the XML document either leads to new tuples being added to the view, or does not affect the view. All the examples considered so far fall into this situation. The cases left out are those when the insert leads to modifying a view tuple. This case will be addressed in Section 3.6.

Algorithm 1 outlines the propagation procedure. Line 1 is performed when v is created, since it is independent of the update. The computation of the $\Delta^+$ tables will be detailed shortly. The core of the complexity in Algorithm 1 lies in line 4: the computation of the remaining union terms.

**Term evaluation based on auxiliary lattice.** Let us now see how to compute the terms that survive pruning. Each such term is sure to involve at least a $\Delta^+$ table, and all but (possibly) one also involve an $R_{\ell}$ table, for some view node label $\ell$. To maintain the view $v$, we rely on a collection of auxiliary data structures which are materialized and also maintained when the data changes. These data structures are organized in a *view lattice*, which is best introduced by means of examples.

Figures 6 and 7 depict the lattices corresponding to the tree patterns shown at the top left of each Figure. For conciseness, in both Figures, the pattern of each node is shown simply by the set of its node labels. Thus, the pattern of the topmost node in Figure 6 is $//aID//bID//cID//dID$, its rightmost child corresponds to the pattern $//aID//cID//dID//eID$ etc. The lattice top node is always the complete pattern, and each pattern node corresponds to one lattice leaf. The view lattice recalls the AND-OR graphs well-known in relational data warehousing [23] adapted to XML tree patterns with multiple return nodes.

Formally, let $v$ be a tree pattern. The lattice of $v$ is a DAG with three categories of nodes: (i) A set of nodes, each labeled by some $P$ pattern. One node is labeled by the pattern $v_{1D}$, obtained from $v$ by annotating all nodes exactly with $ID$. Every other node is labeled by a distinct sub-pattern (itself a tree pattern) of $v_{1D}$. (ii) A set of $\or$-nodes labeled $v$. (iii) A set of join nodes labeled $\or$. Lattice edges trace possible ways of computing some lattice nodes based on nodes below it. For instance, a join ($\or$) allows computing the node labeled $ab$, corresponding to $//aID//bID$, out of the nodes labeled $a$ and $b$ respectively. When the sub-pattern corresponding to a lattice node can be computed in several ways out of the lower nodes, this is modeled by the or ($\or$) node which alone points to the target lattice node. In Figure 6 the sub-pattern $abc$ can be computed in three distinct ways, whereas in Figure 7 there are only two possibilities.

A view lattice captures all view sub-patterns, and possible ways of computing them from one another. Materializing (and maintaining) all these sub-patterns suffices to update $v$ to reflect any insertion. For each union term $t$ to be added to $v$ after an insertion:

- Let $t_R$ be the $\or$ sub-expression(s) of $t$ containing only $R_{\ell}$ occurrences. Then, $t_R$ corresponds exactly to some materialized lattice node(s).
- Let $t_{\Delta^+}$ be the $\or$ sub-expression(s) of $t$ containing only $\Delta^+$ occurrences. Then, $t_{\Delta^+}$ is easily computed based on the new inserted data.

The lattice allows solving the problem of maintaining $v$ based on the “smaller” problems of maintaining sub-patterns of $v$. Given that the maintenance of the lattice leaves is trivial (e.g., replace $R_{\ell}$ by $R_{\ell} \cup \Delta^+$), in theory, this is a solution. However, materializing and maintaining all lattice nodes is likely to be very expensive in terms of space and time. Fortunately, we can focus only on a subset of these nodes:

**Definition 3.11 (Snow Cap).** Let $v$ be a tree pattern. We term snow cap of $v$, any non-empty sub-tree of $v$ such that: for each node $n \in v$ that also appears in $u$, the parent of $n$ in $v$ also appears in $u$.

For instance, in Figure 6 and Figure 7 the boxed nodes depict snow caps. Intuitively, a snow cap copies the root of the pattern and then goes down to some length on all paths, *only including a node if it includes its parent*. This mimics the way mountains are covered by snow, thus the name. We can now state:

**Proposition 3.12.** Let $v$ be a view, $u$ an insertion, and $t$ a resulting term which survives our first pruning (Proposition 3.3). Then, the algebraic expression $t_u$ is exactly the algebraic semantics of a pattern $v_{1t}$ which is a snow cap in $v$’s lattice.

The proof follows directly from Proposition 3.3. For instance, consider the view $v_1$ in Figure 6. For an insertion $u$ to add tuples to $v_2$, one or several of the following cases must hold: (i) $u$ adds a $d$ child to an element on the path $//a//b//c$. The impact of this addition on $v$ is obtained by joining the snowcap $abc$ with $\Delta^+_a$; (ii) $u$ adds a $c$ child to an element matching $//a//b//c$, and this $c$ child has at least one $d$ descendant (join the snowcap $ab$ with $\Delta^+_a$); (iii) $u$ adds a $b$ child to an element matching $//a//b//c$, and this $b$ child has at least one $d$ descendant (join the snowcap $a$ with $\Delta^+_a$); (iv) $u$ adds matches to the full $//a//b//c//d$ view path, and to reflect such additions, no auxiliary structure (lattice node) is needed. A similar analysis of the possible ways in which an insertion could add tuples to $v_2$ in Figure 7 leads to the conclusion that the snow cap nodes in that lattice are necessary and sufficient to maintain $v_2$.

**Proposition 3.13.** Materializing all and only the snow caps of a view $v$ suffices to maintain $v$. Moreover, each snow cap can be maintained based only on other snow caps and the $\Delta^+$ relations extracted during each update.

---

1 We have depicted only the possibilities of computing a pattern by joining mutually disjoint sub-patterns. Clearly, there are more possibilities, e.g., one can compute $abc$ by joining $ab$ with $bc$. We omit this to keep the Figures readable.
From places where they have been inserted. Let holds the IDs assigned to the newly added adding some new scorings and the leaf set, and costs heavily depend on the data, view and update mix. We have materializing a combination of snow caps and leaves, or other lat-

Alternative to snow caps: lattice leaves

Putting it all together. Algorithm 2 (ET-INS) outlines the evaluation of non-pruned terms resulting from insertions. At lines 5 and 6 Algorithm ET-INS relies on structural joins, in order to take advantage of efficient optimization and evaluation techniques provided by the persistent XML store and query engine.

Computing \( \Delta^+ \) relations. Given an insertion \( u \) on the document \( d \) and the view \( v \), Algorithm 3 computes the \( \Delta^+ \) relations. It relies on the functions compute-pul and extr-pattern presented in Section 3.4 to compute the update list, and then to extract \( \Delta^+ \) relations out of the pending updates.

ID-based optimization We now exploit the special properties of Compact Dynamic Dewey IDs to make update propagation even more efficient. Let \( n_1 \) be a view node labeled \( a \) and \( n_2 \) be a descendant of \( n_1 \) in \( v \), labeled \( b \). Consider an update \( u \) such that \( \Delta^+_u \neq \emptyset \). Then, in the union terms involving \( R_a \) and \( \Delta^+_a \), we can replace \( R_a \) by the set of \( a \)-labeled identifiers of the newly added \( b \) nodes. We can do this because the XML ID scheme we use [7] encapsulates in the ID of a node, the IDs and labels of all its ancestors. The IDs of all the \( a \) ancestors of the new \( b \) nodes appear in the new \( b \) nodes’ IDs.

3.6 View tuple modification

In some cases, an insertion on a document \( d \) may lead to modifying existing tuples of a view \( v \). This occurs when the insertion changes the value or the content of an XML node \( n \), whose value (respectively, content) is stored in \( v \). A view tuple storing the value and/or content of \( n \) may also need an update if a descendant of \( n \) is added or modified by the update.

**Example 3.14.** Consider the view \( /a_{1D}/b_{1D} [/c_{1D},cont] \) and an insertion \( u \) adding the XML snippet:
into //d//c. In this case, no $\Delta^+$ relation affects the view, thus no new tuples need to be added. However, the insertion $u$ may lead to modifying some of the $c$.cont values stored by the view, if the intersection //a//b//c and //d//c is not empty.

In the following, we present an algorithm that addresses this case. The algorithm considers all XML nodes for which the view stores content or value, verifies whether that node is affected by the update, and if this is the case, updates its value and/or content.

Algorithm 4: Propagate Insert by Modifying Tuples (PIMT)

Input: insert update $u$, view $v$
Output: updated view $v'$ to reflect $u$

1. $uI = [(n_1,t_1),..., (n_k,t_k)] ← compute-pul(u)$;
2. $cvn ← \{n ∈ v, n annotated with cont or val\}$;
3. foreach tuple $t ∈ v$ do
   4. foreach tuple $(n,t) ∈ uI$ do
      5. foreach node $n ∈ cvn$ do
         6. if $t.n = n$ or $t.n < n$, then
            7. Update $t.n.cont$ (respectively, $t.n.val$) to reflect the insertion of $t_i$

Algorithm (PIMT) starts by computing the pending update lists. It singles out all the content- or value-annotated view nodes, in the node set $cvn$. The algorithm then checks, for each view tuple $t$, whether and how each of the $t$ attributes corresponding to the content or value of a $cvn$ node must change. To that purpose, Algorithm [4] requires that for all $cvn$ nodes, i.e., for all those view nodes for which $cont$ or $val$ is stored, element IDs must be also stored. Based on the IDs, we check whether the node providing the $cont$ attribute in tuple $t$ is the same as, or an ancestor of the modified node $n_i$. If this is the case, then the insertion of $t_i$ has to be propagated to the $t$ attribute corresponding to $n.cont$ (respectively, $n.val$).

It is easy to see that if $cvn$ is empty, insertions cannot modify view tuples (but only add to the view).

If $cvn$ is of size 1 (a single view node stores $val$ or $cont$), then Algorithm PIMT can be implemented by a single efficient structural join (extended to check ancestor-descendant or equality relations) between $v$ and the pending update list. In the view tuples that join with the pending update list, the $cont$ and/or $val$ attributes must be changed.

If $cvn$ contains more nodes, Algorithm (must compare several ID attributes from each view tuple $t$ against the pending update list, and a nested loops join is needed.

We conclude by observing that in practice one cannot know in advance whether an insertion will add or modify tuples, therefore both Algorithms PINT and PIMT are run, based on the pending update list which is computed only once.

4. PROPAGATING DELETIONS

Another possible propagation scenario that we need to consider concerns the case of deletions on a node. Similarly to insertions, deletions may lead to delete an entire view tuple or to modify an existing view tuple. We start by considering the first kind of propagation, i.e., the deletion of tuples from the view.

The general Algorithm that detects and propagates the deletions to the view is similar to the one we have presented for insertions in Section 3. Union terms need to be built and possibly pruned (as shown in Algorithm [5], then evaluated, and this may result into tuples being deleted from the view. We start by presenting some examples.

**Example 4.1.** Consider the view //a//b and the XML document $d$ shown in Figure 8 where the ID of each node is shown as a subscript to the node. Each ID is a sequence of steps, each step holding the label and the relative position of one ancestor of the node.

Consider an update $u_1$ deleting //c//b, which results in the node whose ID is $a_1.c.1.b_1$. Since the view tuple $(a_1,a_1.c.1,b_1)$ had a derivation count of 1, the update leads to removing the tuple from the view.

More generally, given a (subtree) deletion and a label $l$, we term $\Delta^-$ the ordered collection of tuples of the form $(n.id,n.val,n.cont)$ obtained from all deleted nodes $n$ labeled $l$. From the algebraic semantics of the view and the $\Delta^-$ relations, we develop a union of terms much as in Section 3.1 and prune them in similar fashion to Section 3.2.

In some cases, an XML deletion only affects the derivation count of a view tuple, as illustrated below.

**Example 4.2.** Consider the view //a//b and the document $d$ in Figure 8 and an update deleting //c//b.

The view contains a single tuple corresponding to node $a$. The tuple has a derivation count of 2 due to the two $b$ nodes which satisfy the predicate in the view. Therefore, the deletion does not affect the view, since by deleting only the $b$ node identified by $a_1.c.1.b_1$, the $a$ element still has a $b$ descendant. The only effect of the update is to decrease the derivation count by 1.

A subsequent update deleting //f//b will remove the last $b$ of the document and thus remove the tuple from the view. The general
algorithm for propagating deletions by deleting tuples (PDDT) is outlined in Algorithm 5 where Propositions analogous to 3.3 and 3.6 (omitted for space reasons) are exploited in the case of deletions.

A second case occurs when a deletion does not remove tuples from a view, but modifies some value or content attributes. The situation is again very similar to the case when XML insertions modify existing tuples. Accordingly, we have devised an algorithm PDMT (Propagate Delete by Modifying Tuples) which is symmetric to Algorithm 4 and omitted for brevity.

5. EXPERIMENTAL EVALUATION

In this Section, we present a set of experiments on our proposed algorithms. Section 5.1 describes the experimental setting. Section 5.2 studies the performance of our algorithms breaking down detailed running times. Section 5.3 is concerned with scalability when document size varies, Section 5.4 compares our approach with fully recomputing the view (from scratch), finally Section 5.5 compares our approach with the closest competitor [31].

5.1 Settings

We have implemented the PINT and PIMT algorithm described in this paper using Java 6, within our ViP2P Java-based platform (http://vip2p.saclay.inria.fr). ViP2P enables distributed peers to publish XML documents, and to declare materialized views which are filled with results from all network documents, in a symmetric, decentralized publish-subscribe fashion (for our purposes, we only used one ViP2P peer). ViP2P stores view data using BerkeleyDB v4.0.71. For some operations (see below), we rely on the widely known Saxon XQuery processor v9.2.1.1j. All experiments but those described in Section 5.5 were run on a PC with Linux Kubunto v2.6, with a Pentium 4 260GHz CPU and 1GB memory.

Documents, views and queries We use XMark [32] benchmark documents of different sizes. As in [11], we use queries from the (read-only) XMark benchmark as views, and a set of updates derived from the XPathMark benchmark [20] by inserting a dummy element into each of (or deleting, resp.) the nodes returned by the respective XPathMark query. To the extent possible, we used the same queries and updates as in [11], which detected the independence of the updates and the view in most of the cases. Since we are interested in the “other” cases, when updates do affect views, we enhanced the set of updates with more path expressions from the A and B subsets of the XPathMark benchmarks (the names of these queries start with the respective letter). Finally, we also added a set of path expressions of our invention, whose names start with X.

For space reasons, we report only on the results obtained with XML insertions, i.e. running algorithms PINT (Section 5.3) and PIMT (Section 5.6).

Implementation details We use Saxon for the first step of our approach, namely identifying the target update nodes that will receive new children. To actually update the document, we build the pending update list, add the new children to the target nodes using Saxon’s in-memory operations, and then serialize the modified document again using Saxon.

To update the view, we extract the $\Delta^+$ tables from the pending update list and apply all the respective steps described in Section 5. We store the necessary auxiliary structures (the snow cap lattice nodes described in Section 5.5) as ViP2P views.

All algebraic operations (notably joins) are performed using ViP2P’s physical operator library. We stress that ViP2P is a Java-based prototype and improvements by constant factors could probably be obtained by further optimizing the code, using C++ etc. Nevertheless, we implemented all algorithms in the same framework, and relied on state-of-the art algorithms, e.g., for structural joins. Thus, we believe our experiments accurately highlight the various performance trade-offs involved.

Measured times In the following, we report on a set of times which were averaged over five executions. Find Target Nodes is the time taken by Saxon to identify the nodes involved by an update operation. Compute Delta Tables is the time taken to build the $\Delta^+$ tables starting from the inserted XML fragments. Get Update Expression is the time to build, unfold, and prune the algebraic expression corresponding to the updates to be propagated. Execute Update is the time to evaluate the expression thus obtained within ViP2P’s algebraic XML query evaluation engine. Update Lattice is the time to update the auxiliary data structures (snow cap lattice terms) by computing the necessary tuples and adding them into BerkeleyDB.

5.2 Performance of the incremental maintenance algorithms

To gauge the effectiveness of our algorithms, we have run a set of experiments by using as views the queries $Q_1$, $Q_2$, $Q_3$, $Q_4$, $Q_6$, $Q_8$, $Q_{13}$ and $Q_{17}$ of the XMark [32] benchmark. For each query,
we have employed a set of update path expressions (as described above), divided into five classes: (c1) Linear path expressions; (c2) path expressions with an And predicate; (c3) path expressions with an Or predicate; (c4) path expressions with an AO (and-or) predicate; (c5) Boolean path expressions.

Figure 9 shows for each pair (view, update) the impact of the view maintenance time. It can be observed that in all cases the times to Compute Delta Tables, Get Update Expression and Execute Update are smaller than the time to locate the target nodes. As expected, the latter times depend on the target XPath expression of the updates. Thus, for instance, the evaluation of a long linear path expression is slower than for a path expression with an AND or OR filter. Moreover, the absolute value of the time to Update Lattice depends on the complexity of the view considered and less on the specific update applied. For views like Q3 (FLWR expression with conditions), it almost stays steady while increasing the complexity of the update path expression from class (c1) to (c5).

Lastly, Figure 10 shows the performance results for all the XMark views considered, by summing up the Find Target Nodes, Compute Delta Tables, Get Update Expression, Execute Update and Update Lattice times.

5.3 Scalability wrt. Source Document Size

We then performed a scalability test for our algorithms, to check how they perform on larger source documents. We have employed various document sizes ranging from 500KB to 10MB, and have observed their performance, as shown in Figure 11 where the y axis is in logarithmic scale. The cost of updating the lattice (i.e., the auxiliary structures) is the most significant component of the view update costs, while the delta table computation and the time to get the update expression are comparably small. Moreover, executing the update, i.e., computing the join expressions which determine which tuples should be added to the view, has a cost that grows reasonably with the document size, and follows the same trend of the cost of finding target nodes. This experiment shows that the cost for view maintenance is beneficial for all the document sizes up to 10MB. Additional experiments shown below and comparing with full view recomputation will further confirm this claim.

5.4 Comparison with Full Re-computation

We have conducted an experiment to measure the gain that our incremental algorithms have over the baseline when the view is fully recomputed from the modified document. This experiment aimed to show the time necessary to incrementally update a view, by exploiting snowcups and pruning the term expression, versus the time necessary to compute the full unioned term expression without pruning and without relying on the lattice at all. Figure 12 shows the results for each view-update pair.

It can be noticed that the full expression recomputation becomes prohibitive for many of the scenarios, while the incremental view maintenance achieves much lower times.

5.5 Comparison with Previous Algorithm

In order to show the benefit of bulk updates for incremental view maintenance, in our framework we have re-implemented IVMA, the view maintenance algorithm described in [31]. This algorithm propagates to XPath views, updates which add or delete exactly one node at a time. For this experiment, we used insertions which add a fixed XML tree, consisting of a root node with four children. Such an insertion is handled in one shot by our algorithm, and by five consecutive calls to IVMA in [31]. These experiments have been executed on a Linux 2.6.31.13-server-1mb, with 2.33GHz Intel(R) Xeon(R) CPU 5140 and 4GB memory. Figure 13 (in logarithmic scale) shows that our approach outperforms IVMA by (at least) one order of magnitude for the view Q1, and a source document of 100KB.
5.6 Impact of Auxiliary Structures

Finally, we have tried to quantify the trade-offs between using the snow caps, respectively the leaves of the lattice as auxiliary structures. Figure 14 shows the time to build lattice nodes, and the space occupancy, for one view Q2.

For the various sizes of the source documents, the time to build (respectively, size of) the lattice snow cap nodes are by one order of magnitude higher than the time to build (respectively, size of) only the lattice leaves. This confirms the benefit of using the latter in the computations associated to incremental view maintenance.

6. RELATED WORK

A large body of past research has been devoted to view updates in the context of relational databases [8, 14, 21, 22, 8, 21] focus on the view update problem, i.e., on how to translate a view update into a database update, while avoiding the presence of inconsistencies and side effects on the view. Recently, [14] proposed update policies, expressed in a bidirectional language, to guarantee that the view update is well behaved and handles arbitrary changes to the view. Optimal incremental view maintenance algorithms for relational and deductive database systems were presented in [22], where the notion of derivation count for each tuple in the view is introduced. The algorithms addressed consider both recursive and non-recursive views. In both cases, view definitions are used to generate a set of rules that compute the changes to the views using the base relations and the old views.

In the context of the XML data model, quite recently, [13] studied the problem of incremental view maintenance in its Boolean version and with respect to the XPath language. Boolean incremental view maintenance checks that, after applying the update to the base data, the XPath expression representing the view is still satisfied. Similarly to our approach, they studied the above problem and derived its complexity per update, i.e., by considering one update at a time. The view language they consider is slightly more limited than ours (in particular, they do not support multiple returning nodes), and their approach does not consider incorporating efficient XML query processing techniques in the view update process.

A practical fragment of XPath with \(/, //, *, []\) has been used in previous work on incremental view maintenance for XPath [30, 31]. Interestingly, they also consider count() predicates, therefore view maintenance may be non-monotonic: adding some XML nodes may lead to removing data from the view, while removing XML nodes may add data to a view. In contrast, our conjunctive tree pattern dialect is monotonic. Compared to [31], we focus on (i) tree patterns with multiple return nodes, which cannot be handled by the approach of [30, 31] (based on the analysis of the XPath “view main path”). Views with multiple return nodes may lead to very efficient multiple-view rewritings [26]; and (ii) bulk updates, where several nodes can be added at the same time. As we have argued in the Introduction, the XQuery Update language gives many opportunities for such updates. Moreover, our experiments demonstrated that our algorithms, leveraging state-of-the-art techniques in XML query evaluation, outperform repeated application of the node-based algorithm of [31].

An extension of [31] is [30] which considers the case when the database and the view store are decoupled and the update has to be propagated using less information. The XPath dialect and node-at-a-time approach stay the same as in [31].

To the best of our knowledge, the only works which study the incremental view maintenance problem for XQuery views are [17, 18, 19], [17, 18] focus on the maintenance of XQuery views over relational data. The algorithms of [19] translate updates through views expressed in the internal tree algebra of Galax. This approach is elegant due to its usage of an algebra, and handles a significantly richer XQuery subset than we do in this work. However, its tree-oriented algebra makes it differ significantly from our more traditional approach based on structural joins, delta tables, and term pruning heuristics. Moreover, it is placed at a higher level and does not consider practical aspects related to the efficient implementation of the propagation algorithms in a generic XML data management platform.

A close work in this area [1] considers the maintenance of tree pattern views (with some non-monotonic extensions) over active documents, that is, XML documents including calls to Web services, which return streams of answers that are inserted in the document. The solution consists of algorithms to be applied when each new answer is received and inserted in the document, a hybrid granularity between node-level (since an answer can contain several nodes) and statement level (since they do not use declarative update statements). Their solution relies on Datalog optimization techniques and an XML database used as a black box, whereas we describe algorithms to be implemented inside the engine.

An important line of related works seeks to identify when a view is unaffected by an update [9, 11, 12]. In contrast, we provide algorithms for propagating the insertions when the view is affected.

Finally, the complexity of evaluating (XPath) tree patterns has been first established in [23].

7. CONCLUSION AND FUTURE WORK

In the current paper, we have devised algebraic incremental view maintenance algorithms, that work on a per-statement basis, as opposed to previous per-node approaches. By leveraging structural IDs and appropriate auxiliary data structures called snowcaps, our technique is efficient and scalable at the same time.

Future work is devoted to extend our approach to other XML update operations and to apply our algebraic techniques to the XML view update problem.

8. REFERENCES

Figure 14: Time to build (and size occupied by) the snowcaps, respectively, the lattice leaves for the XMark views $Q_2$.