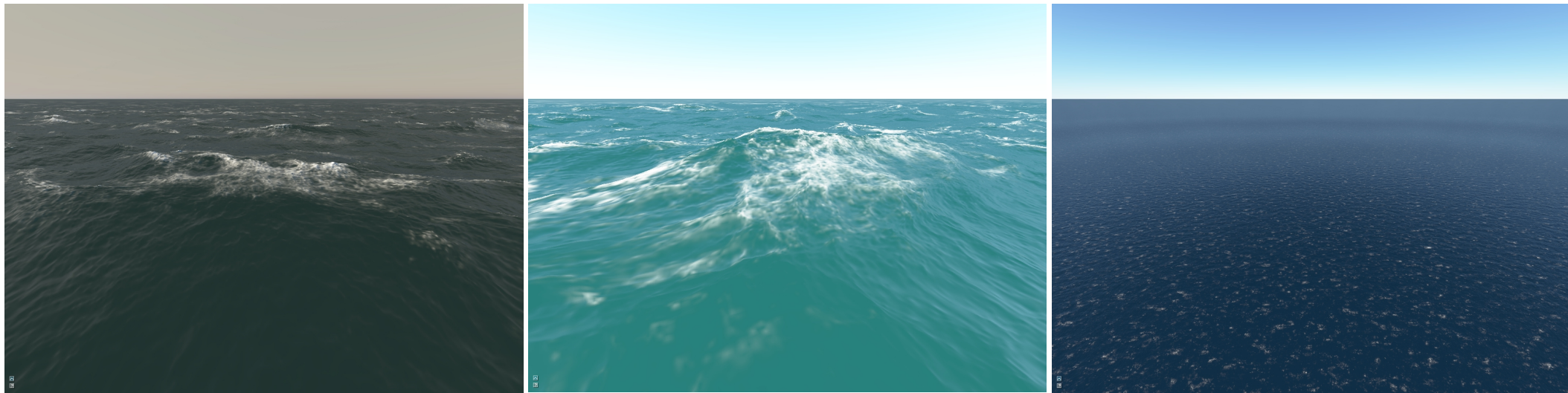


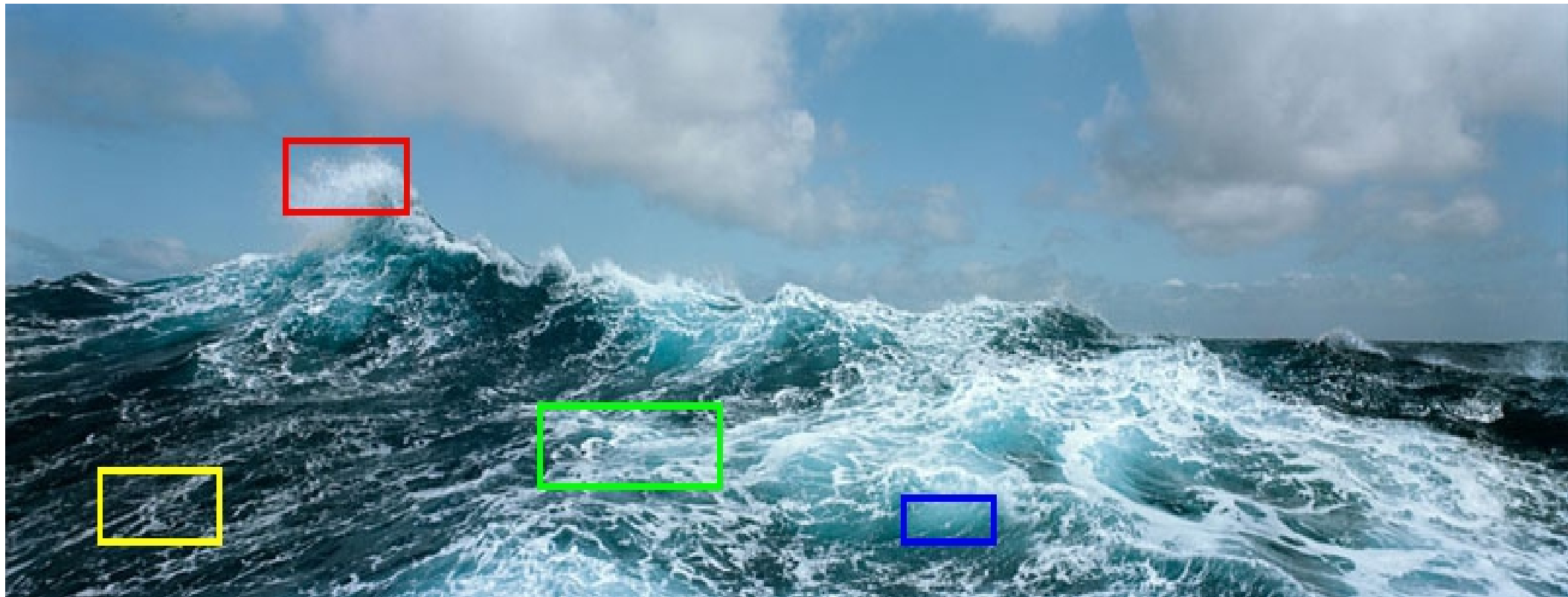
Real-time Animation and Rendering of Ocean Whitecaps



Jonathan Dupuy, Eric Bruneton

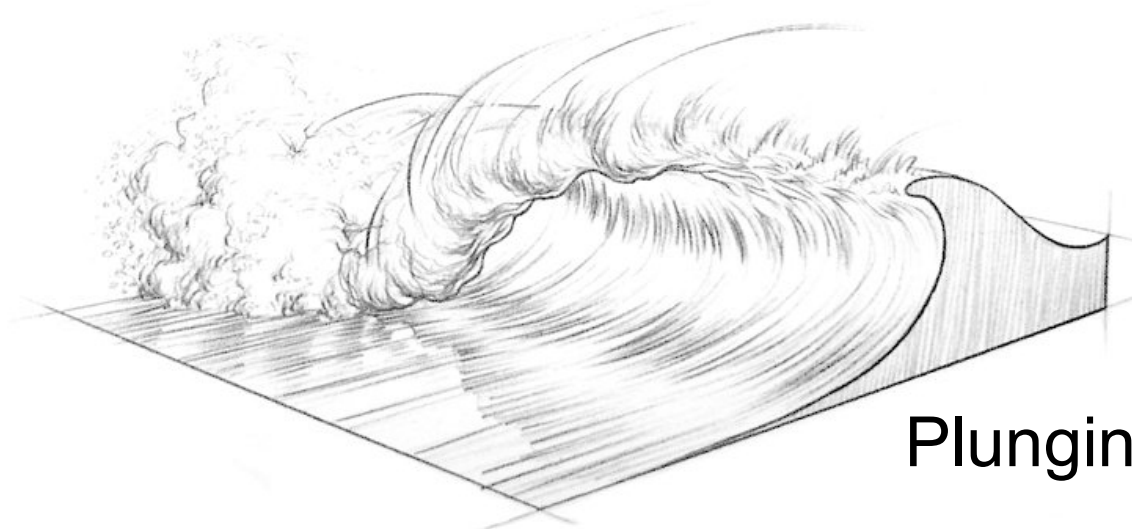
INRIA Grenoble Rhône-Alpes, Université de Grenoble et CNRS, Laboratoire Jean Kuntzmann
Université de Lyon, CNRS Université Lyon 1, LIRIS, UMR5205, F-69622, France

Whitecaps

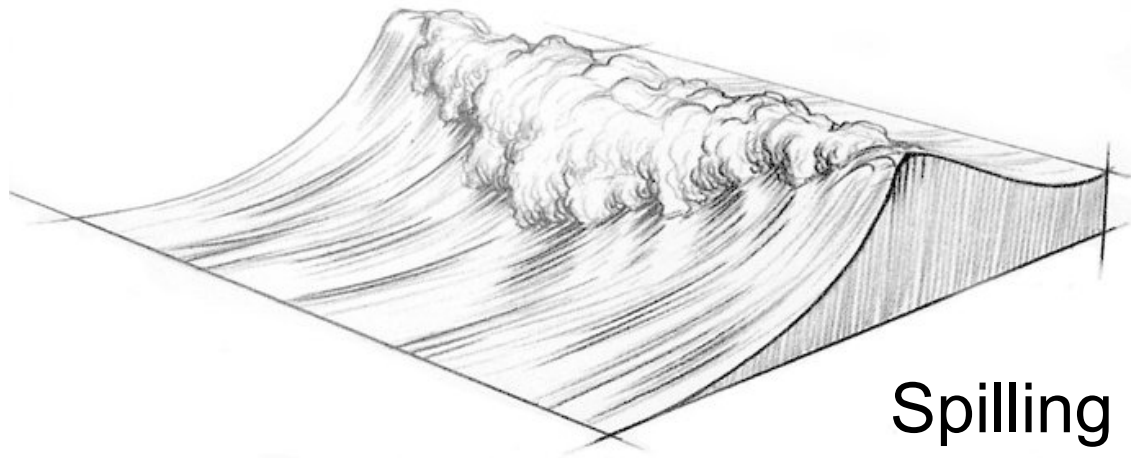


spume + **foam streaks** + **surface foam** + **bubble cloud**

Deep Water Breaking Waves



Plunging breaker



Spilling breaker

Motivation

Real time



Photographs



Movies



Ocean Rendering: Wave Models

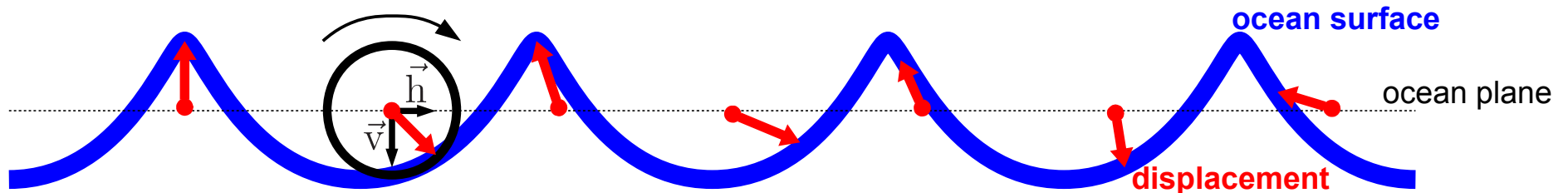
Trochoidal waves



Fourier transform



ocean surface = horizontally and vertically undulated plane

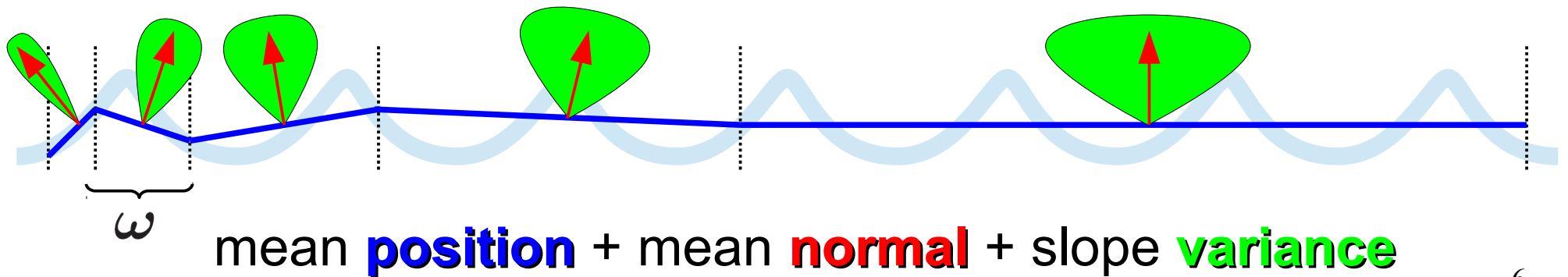


Ocean Rendering: Lighting



$$I(\omega) = \boxed{I_{\text{sun}}(\omega)} + \boxed{I_{\text{sky}}(\omega)} + \boxed{I_{\text{water}}(\omega)}$$

The equation is annotated with icons: a yellow arrow pointing to a wavy blue line under $I_{\text{sun}}(\omega)$; clouds and a wavy blue line under $I_{\text{sky}}(\omega)$; and a wavy blue line with blue arrows pointing upwards under $I_{\text{water}}(\omega)$.

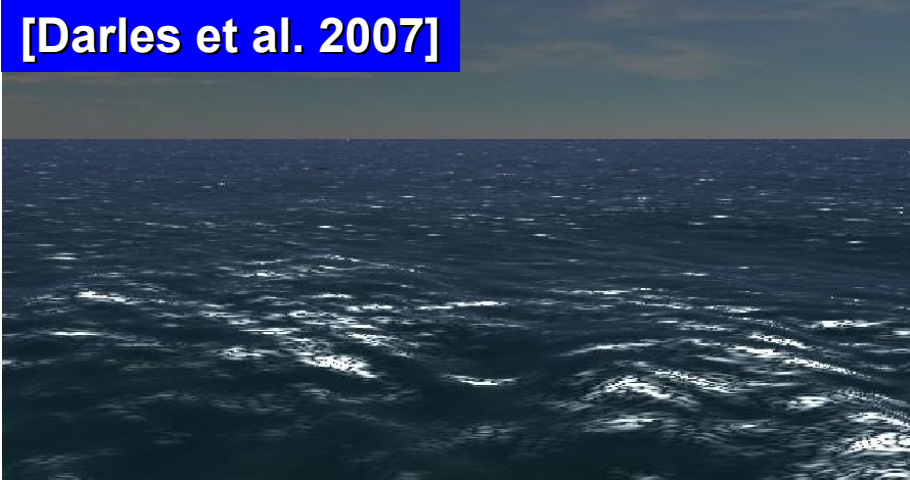


Ocean Rendering: Whitecaps

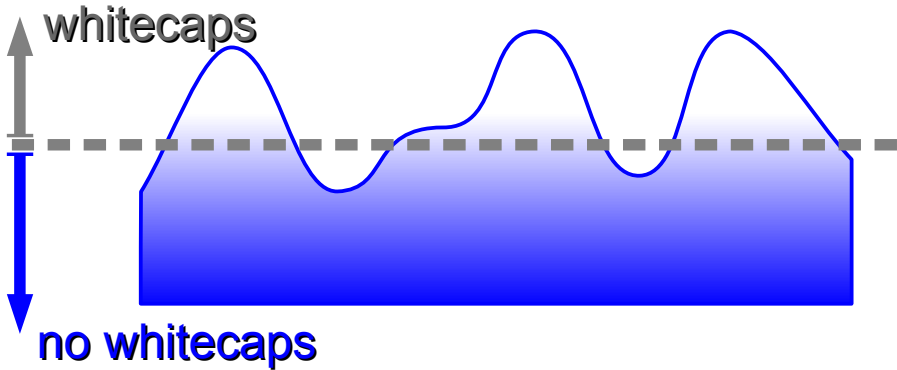
Empirical models

Particle based

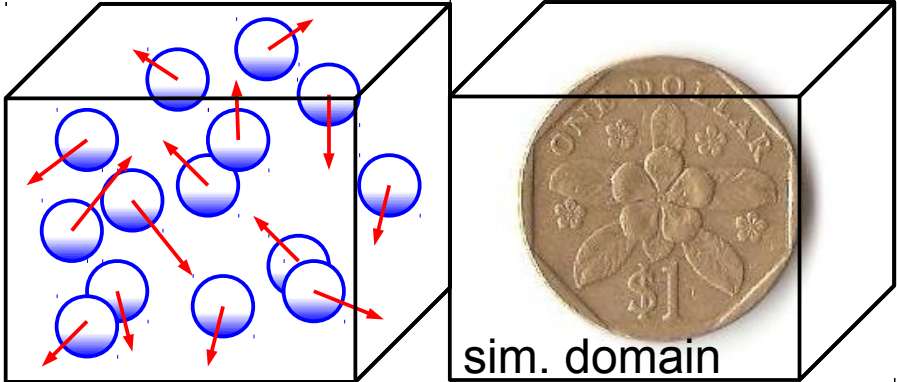
[Darles et al. 2007]



[Chentanez and Müller 2011]



low quality



no control / slow

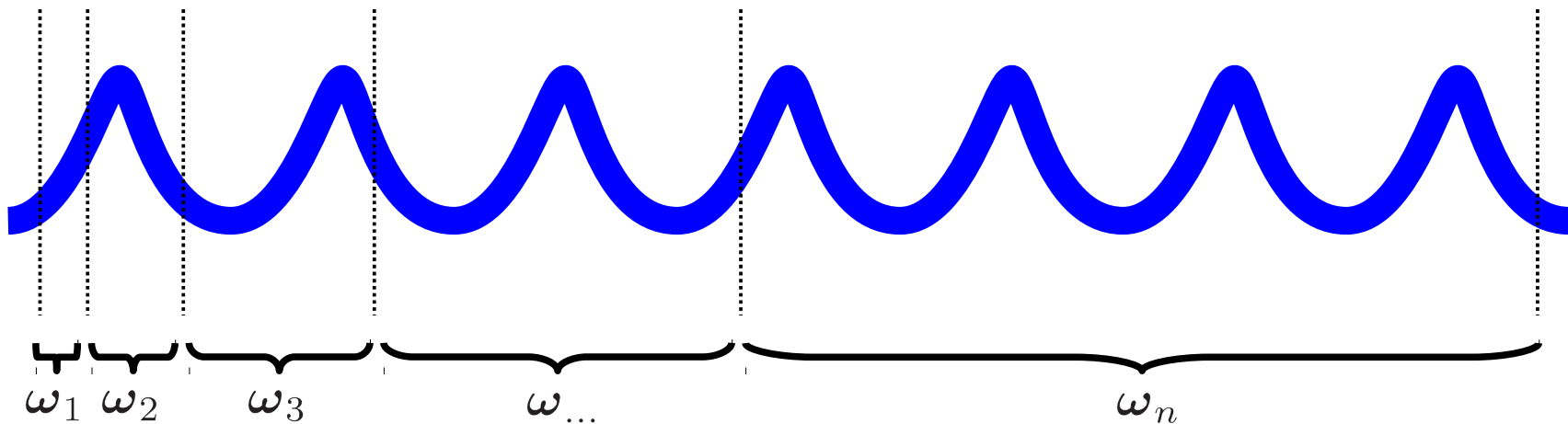
Objective

- Extend Bruneton's lighting model to account for whitecaps
 - Any viewpoint from ground to space
 - Seamless transitions from geometry to BRDF
 - Real time
- Context
 - Deep water waves
 - Gaussian heights and slopes
 - Spilling breakers only (no overturning)

Ocean Lighting

[Bruneton et al. 2010]

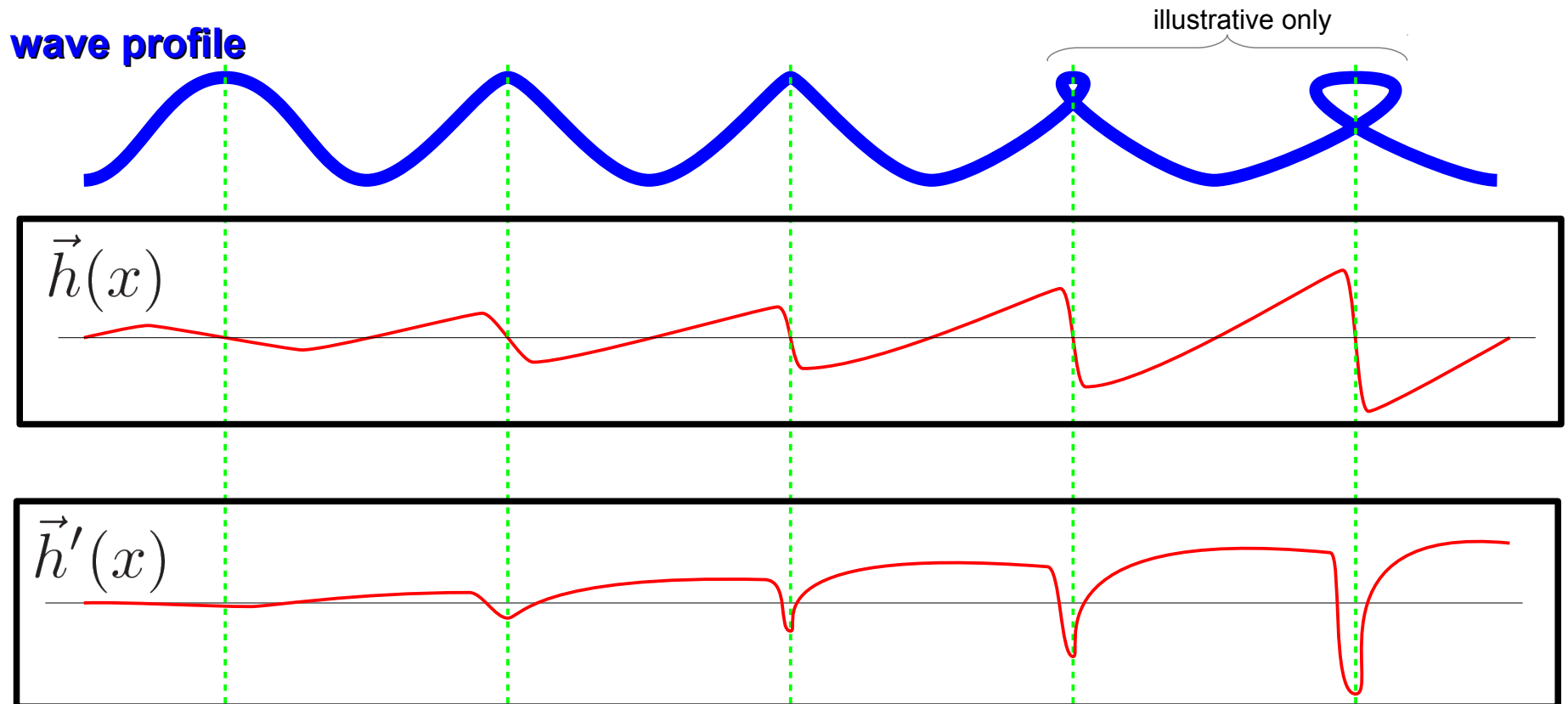
- $I \approx \boxed{I_{\text{sun}} + I_{\text{sky}} + I_{\text{water}}} + \boxed{I_{\text{whitecap}}}$
- Whitecap radiance depends on amount of breaking waves $W \Rightarrow I_{\text{whitecap}} = W \cdot \text{Lambert}_{0.4}$



⇒ $W(\omega), \forall \omega ?$

Breaking Waves

- Use surface tension
 - Proportional to jacobian of horizontal displacements



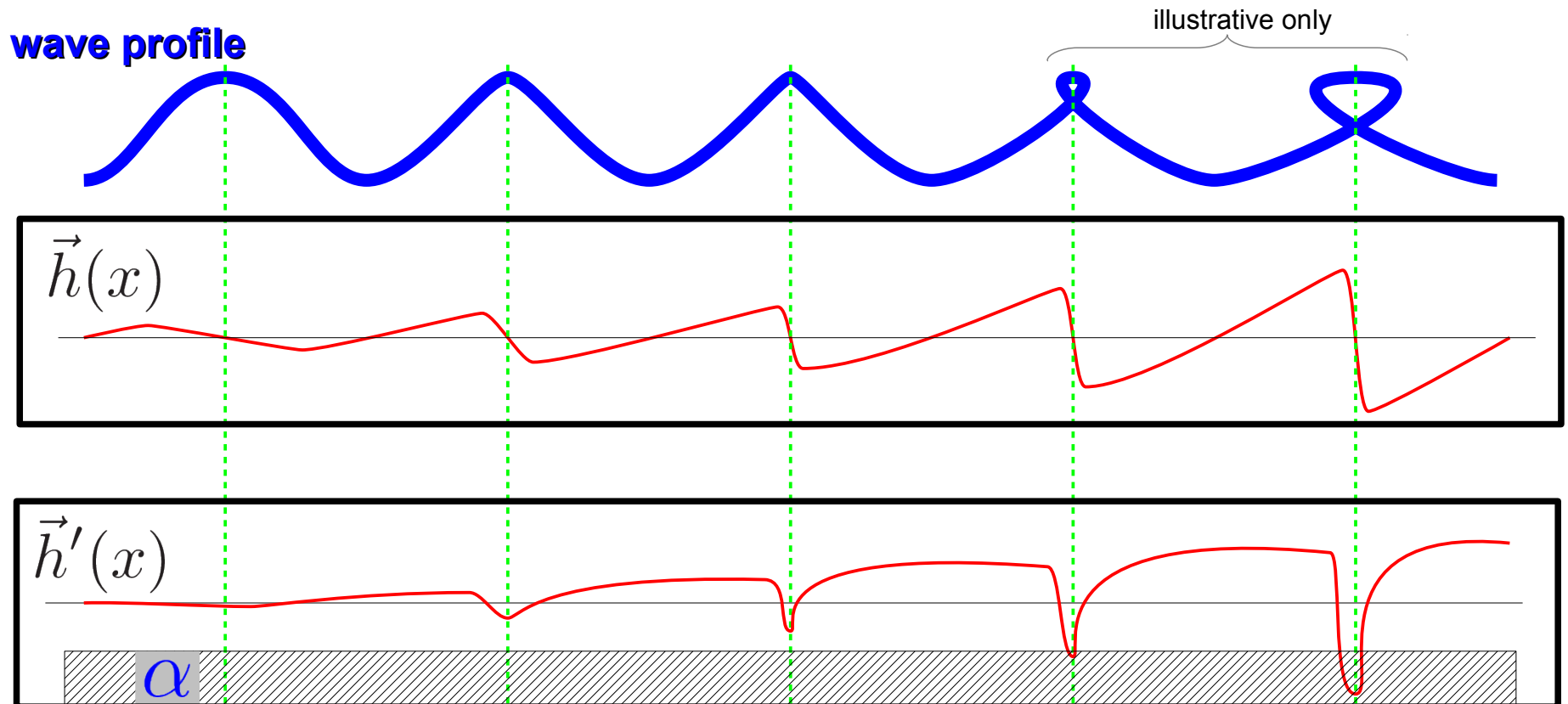
Breaking Waves

- We use

$$W(\omega) = \int_{\omega} H(\mathbf{p}) d\mathbf{p}, \quad H(\mathbf{p}) = \begin{cases} 1 & \text{if } J(\mathbf{p}) < \alpha \\ 0 & \text{otherwise} \end{cases}$$

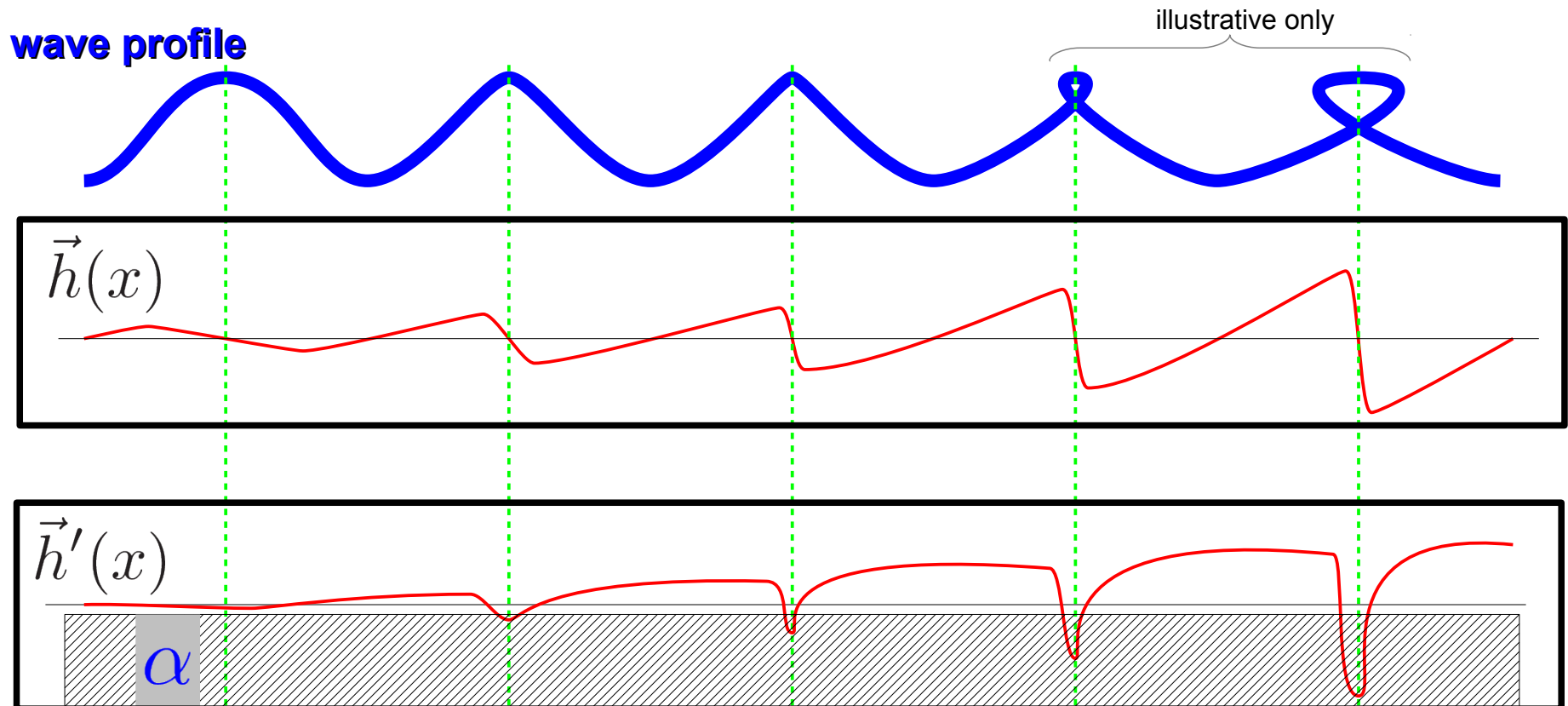
Breaking Waves

- Use surface tension
 - Proportional to jacobian of horizontal displacements



Breaking Waves

- Use surface tension
 - Proportional to jacobian of horizontal displacements



Breaking Waves

- We use

$$W(\omega) = \int_{\omega} H(\mathbf{p}) d\mathbf{p}, \quad H(\mathbf{p}) = \begin{cases} 1 & \text{if } J(\mathbf{p}) < \alpha \\ 0 & \text{otherwise} \end{cases}$$

- $H(\mathbf{p})$ depends on Gaussian functions

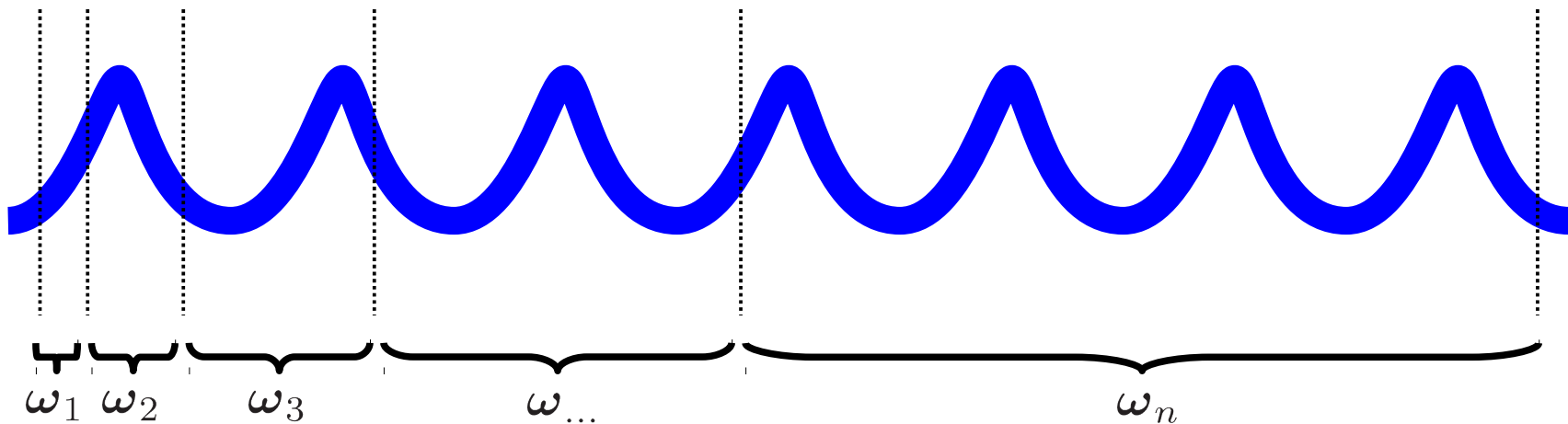
$$\begin{aligned} W(\omega) &\approx \frac{1}{\sqrt{2\pi\sigma_{\omega}^2}} \int_{-\infty}^{+\infty} H(\mathbf{p}) \exp\left[-\frac{(J(\mathbf{p}) - \mu_{\omega})^2}{2\sigma_{\omega}^2}\right] dJ(\mathbf{p}) \\ &= \frac{1}{2} \left[1 + \operatorname{erf}\left(\frac{\alpha - \mu_{\omega}}{\sqrt{2\sigma_{\omega}^2}}\right) \right] \end{aligned}$$

$\mu_{\omega}, \sigma_{\omega}^2$ parameters can be computed analytically for trochoids or through hardware mipmapping for Fourier waves

Ocean Lighting

[Bruneton et al. 2010]

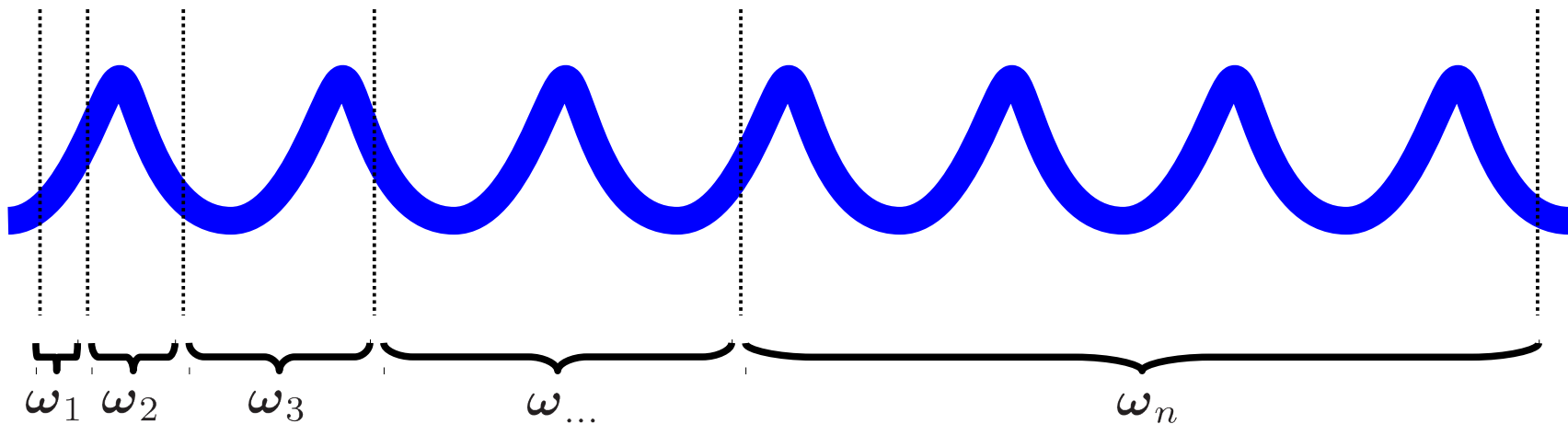
- $I \approx \boxed{I_{\text{sun}} + I_{\text{sky}} + I_{\text{water}}} + \boxed{I_{\text{whitecap}}}$
- Whitecap radiance depends on amount of breaking waves $W \Rightarrow I_{\text{whitecap}} = W \cdot \text{Lambert}_{0.4}$



⇒ $W(\omega), \forall \omega ?$

Ocean Lighting

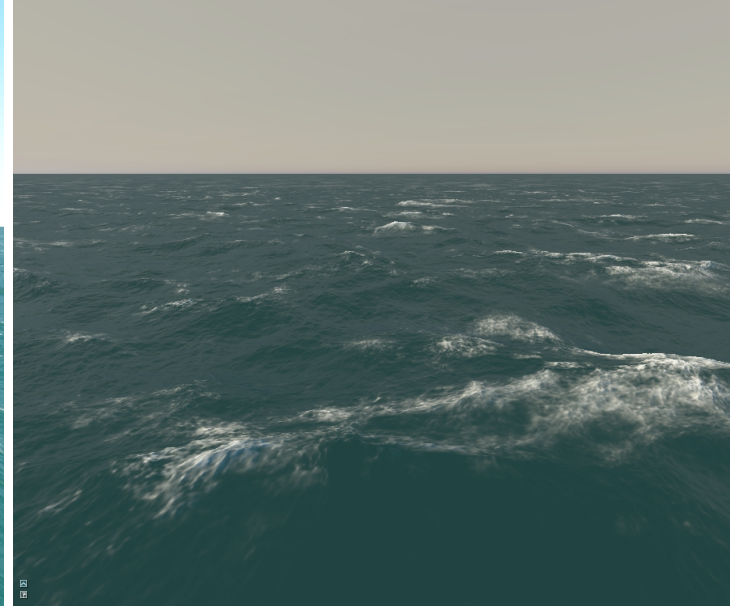
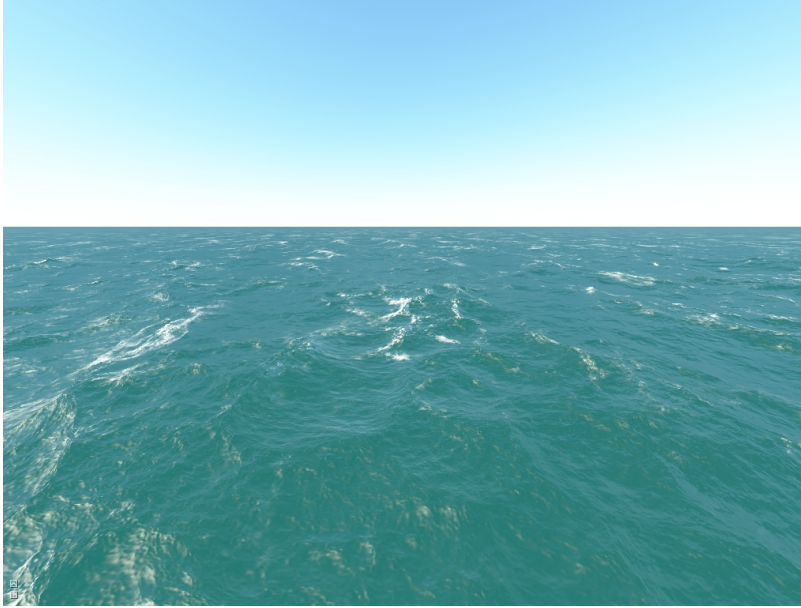
- $I \approx I_{\text{sun}} + I_{\text{sky}} + I_{\text{water}} + I_{\text{whitecap}}$
- Whitecap radiance depends on amount of breaking waves $W \Rightarrow I_{\text{whitecap}} = W \cdot \text{Lambert}_{0.4}$



➡ $W(\omega) = \frac{1}{2} \left[1 + \text{erf} \left(\frac{\alpha - \mu_{\omega}}{\sqrt{2\sigma_{\omega}^2}} \right) \right]$

Results: Quality

real time

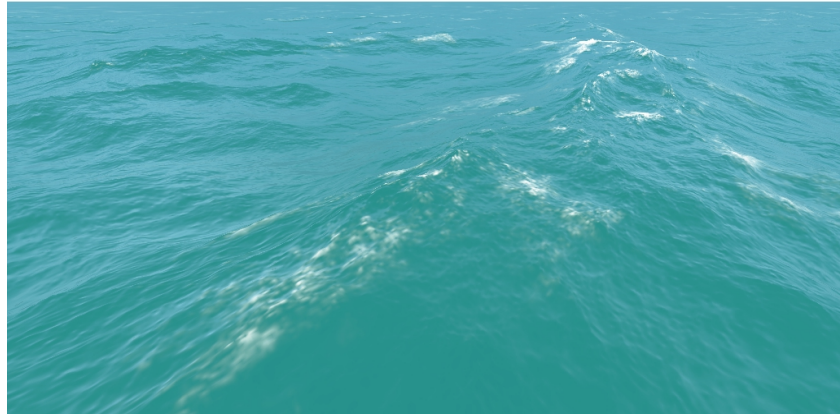


photographs

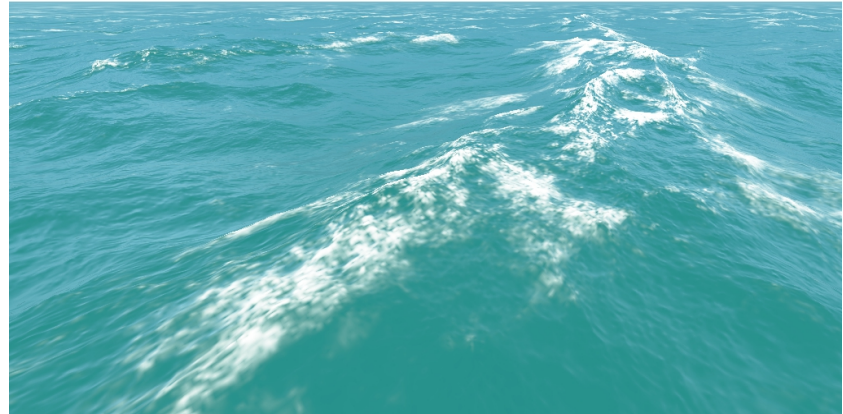


Results: Control

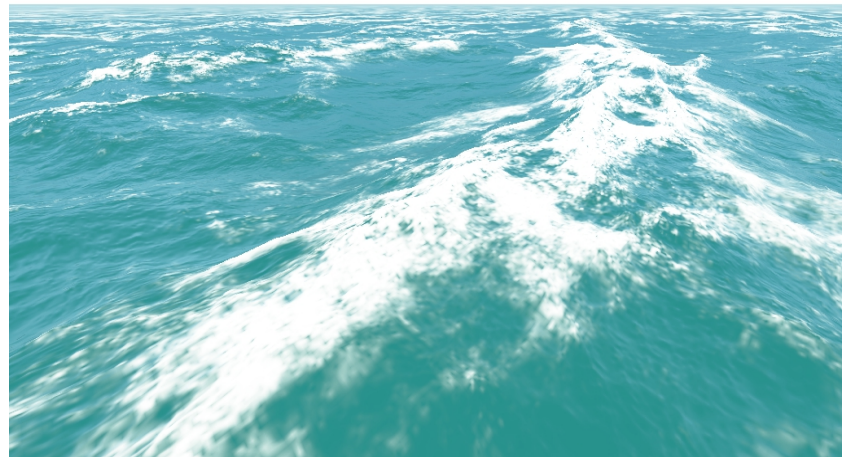
$$\alpha = -0.1$$



$$\alpha = +0.3$$

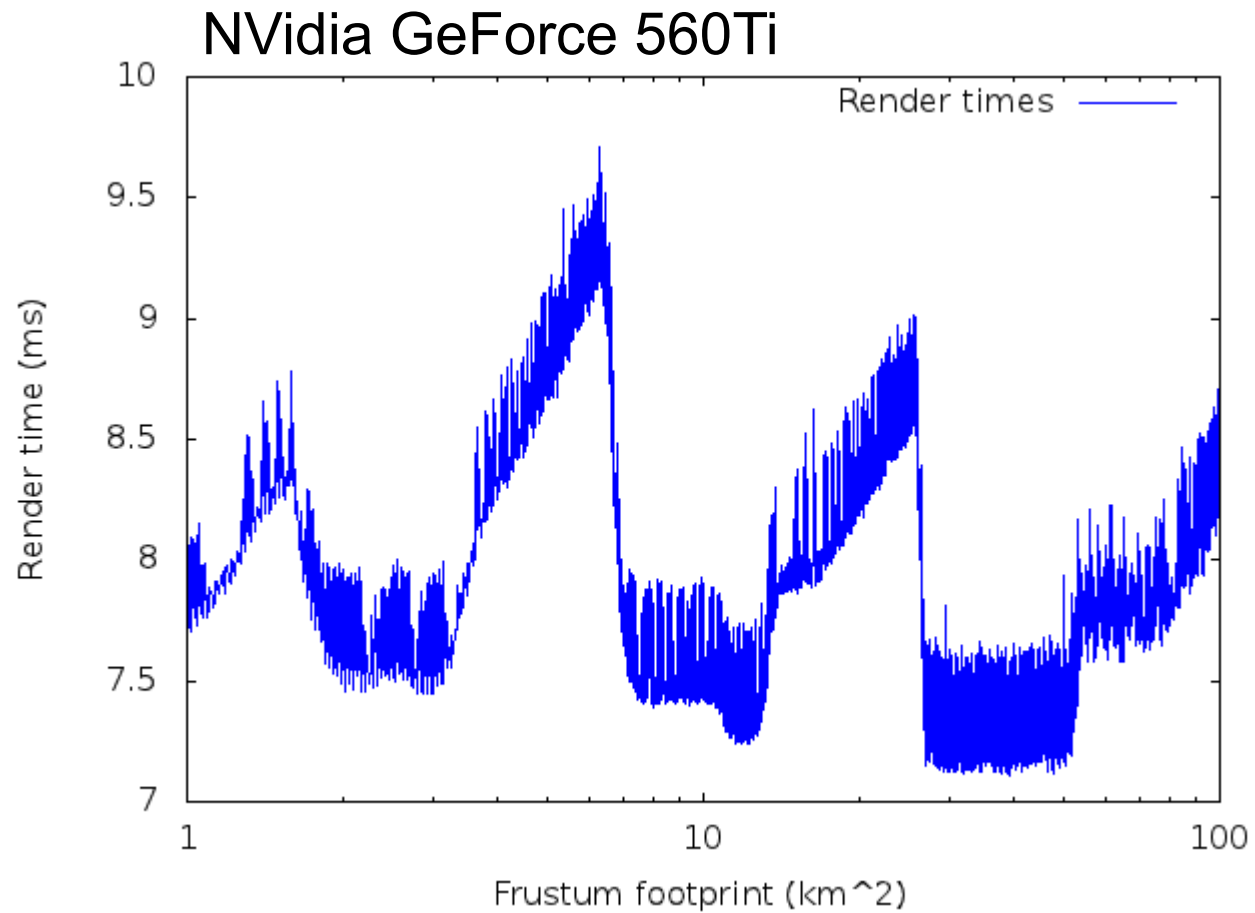


$$\alpha = +0.7$$



(same surface)

Results: Scalability / Real Time



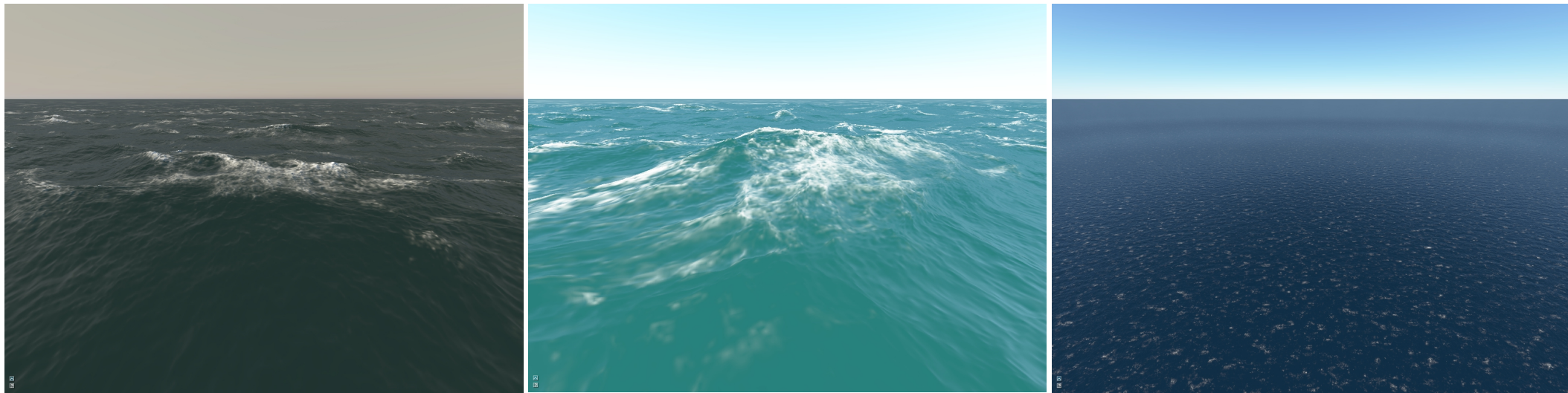
Results: Limitations

- Reflectance fluctuations only
 - No impact on geometry
ex: no plunging breakers
- No decay
 - Whitecap can last several seconds
- Analytical surface
 - Repetitive artifacts on periodic surfaces

Conclusion

- Ocean scenes with whitecaps in real time
 - Scalable performance
 - Controlable
 - Good quality
- Future work
 - Decay
 - Richer whitecap shading model (currently Lambertian / no visibility)

Real-time Animation and Rendering of Ocean Whitecaps

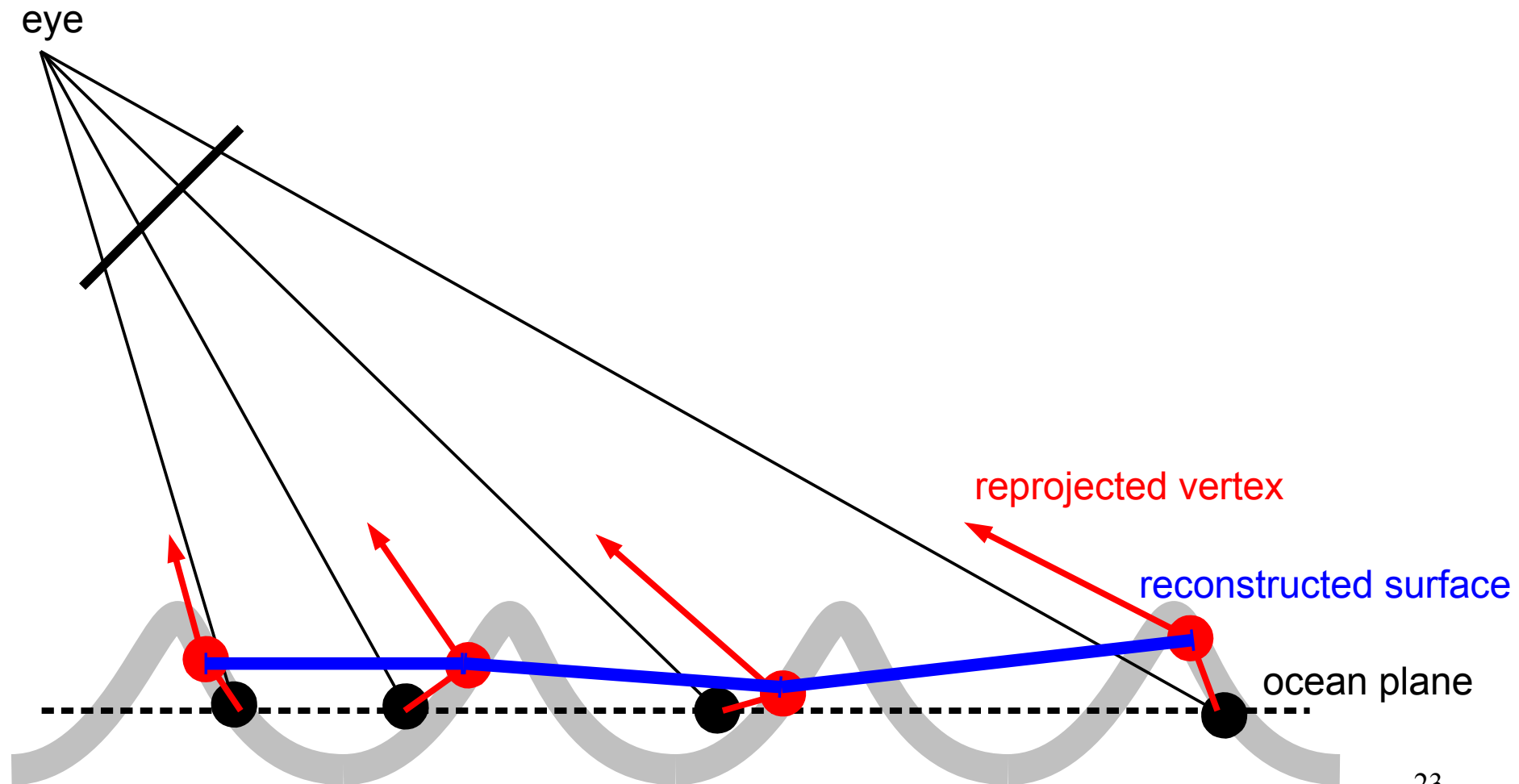


Jonathan Dupuy, Eric Bruneton

INRIA Grenoble Rhône-Alpes, Université de Grenoble et CNRS, Laboratoire Jean Kuntzmann
Université de Lyon, CNRS Université Lyon 1, LIRIS

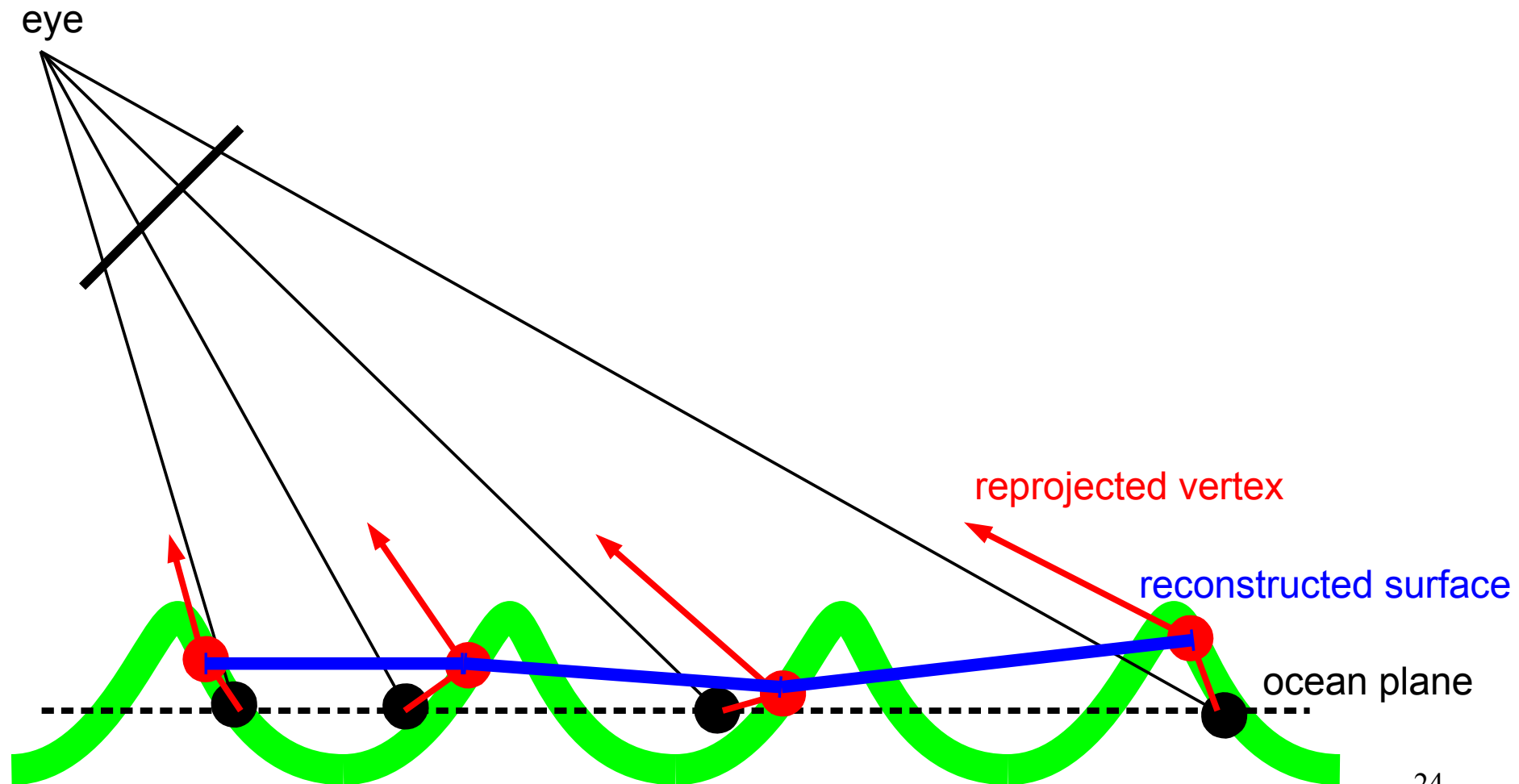
Projected Grid

- Automatic geometrical LOD

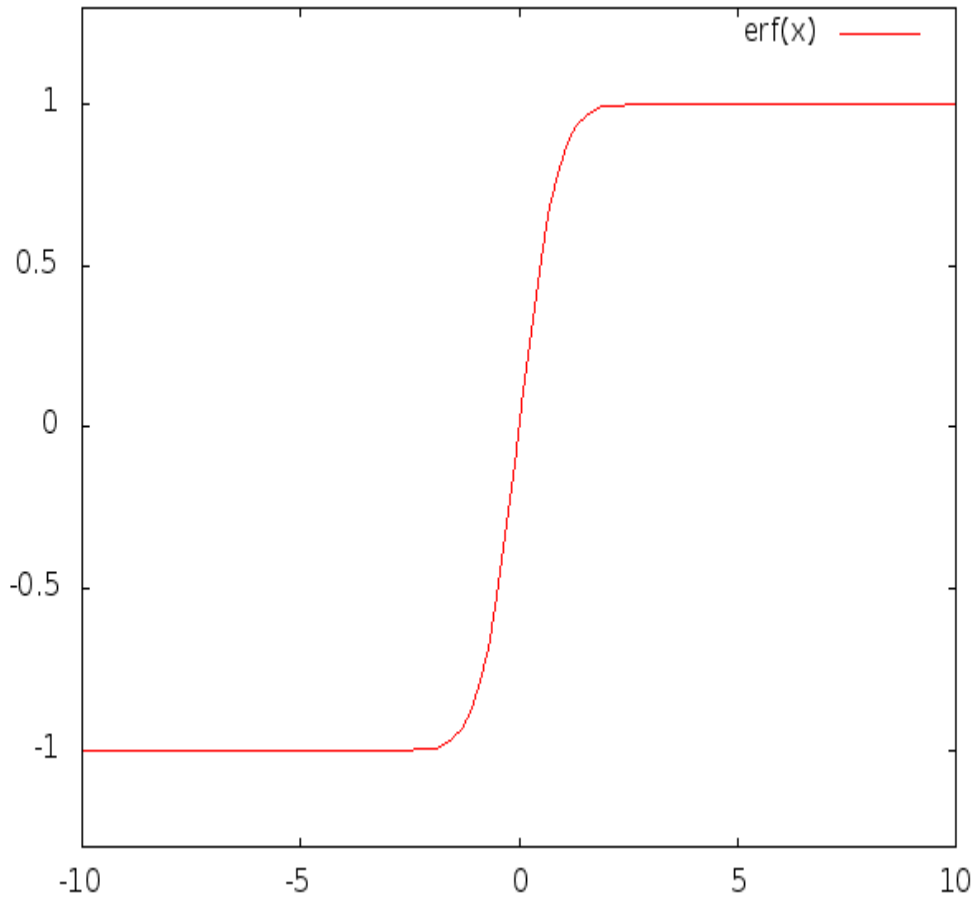


Projected Grid

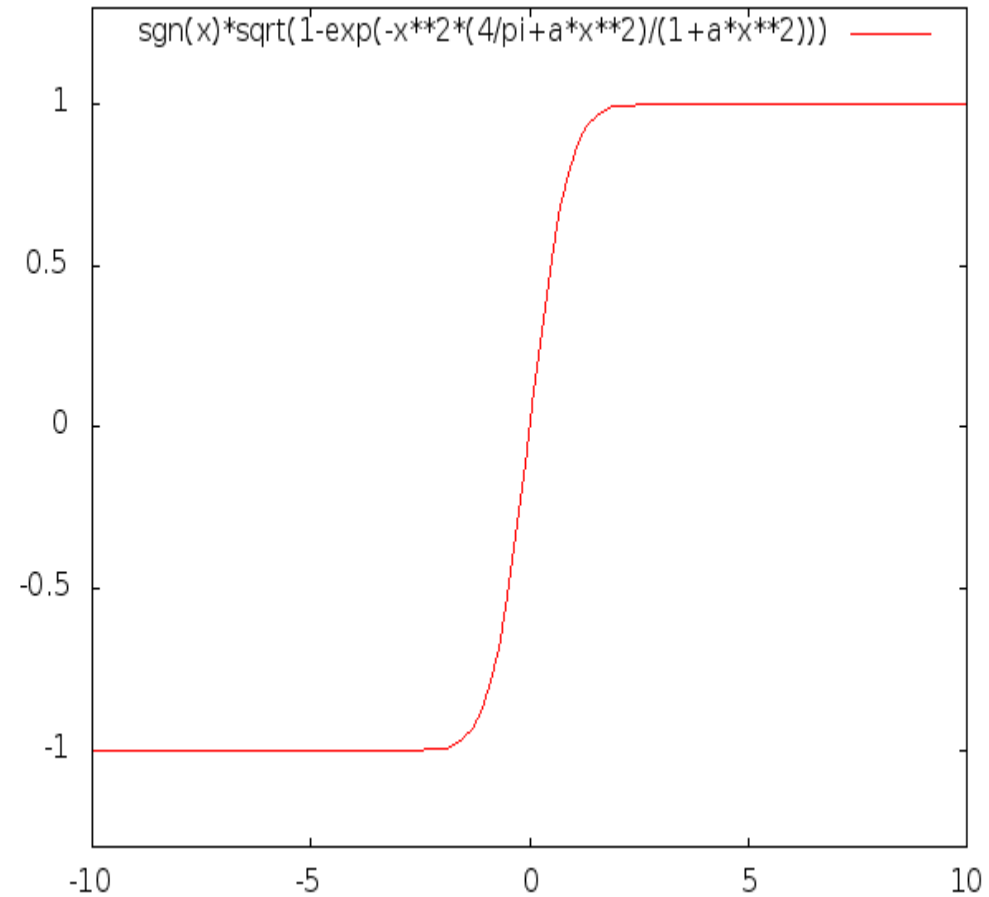
- Automatic geometrical LOD



Erf: Approximation

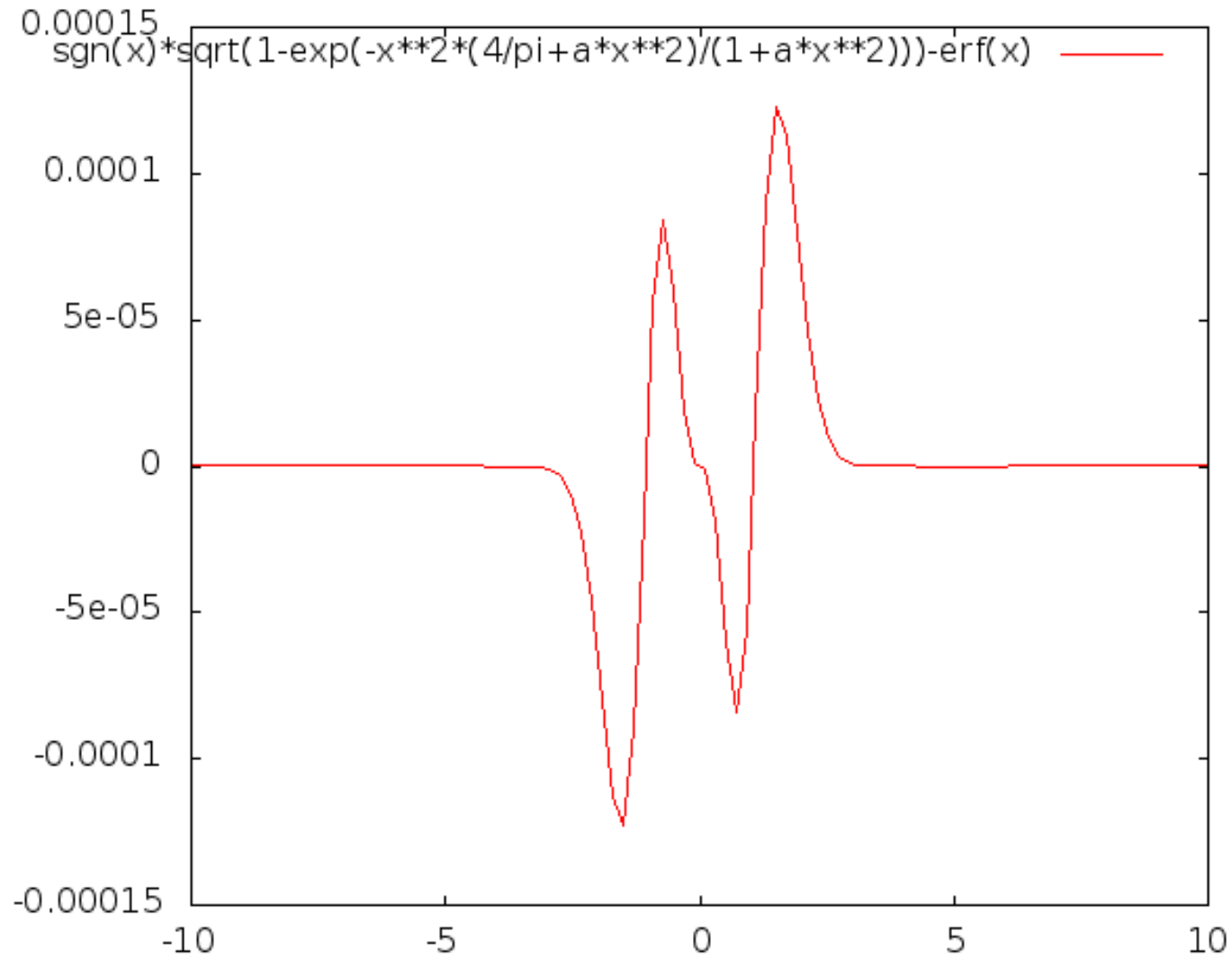


$\text{erf}(x)$



our approximation

Erf: Error



max error: 0.00012